Characterizing floods in the poorly gauged wetlands of the Tana River Delta, Kenya, using a water balance model and satellite data

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Abstract. Wetlands, such as those of the Tana River Delta in Kenya, are vital but threatened ecosystems. The flooding characteristics of wetlands largely determine their physical, chemical and biological properties, so their quantification is crucial for wetland management. This quantification can be achieved through hydrological modelling. In addition, the analysis of satellite imagery provides essential hydrological data to monitor floods in poorly gauged zones.

The objective of this study was to quantify the main water fluxes and flooding characteristics (extent, duration and number of floods) in the poorly gauged Tana River Delta in East Africa during 2002–2011. To do so, we constructed a lumped hydrological model (the Tana Inundation Model, TIM) that was calibrated and validated with MODIS data. Further analysis of the MYD09A1 500 m composite product provided a map of the empirical probability of flooded state. In non-extreme years and for the current topology of the delta, the flood extent exceeded 300 km\textsuperscript{2}. Floods over 200 km\textsuperscript{2} occurred on average once a year, with a mean duration of 18 days. River discharge from the upper basin counted for over 95% of the total water inflow. The results are discussed in the light of possible improvements of the models and wetland management issues.

This study provides the first known quantification of spatial and temporal flooding characteristics in the Tana River Delta. As such, it is essential for the water and natural resource management of the Tana River basin. The water balance approach was pertinent to the study of this system, for which information on its internal properties and processes is limited. The methodology, a combination of hydrological modelling and flood mapping using MODIS products, should be applicable to other areas, including those for which data are scarce and cloud cover may be high, and where a medium spatial resolution is required.

1 Introduction

Wetlands are increasingly recognized as ecosystems that are essential to human activities (Mitsch and Gosselink, 2000) because they provide a wide range of ecosystem services (Daily, 1997; Millennium Ecosystem Assessment, 2005). However, they are amongst the most threatened ecosystems worldwide (Vitousek et al., 1997). Their extent is rapidly declining, with an estimated decrease in the global average maximum inundated area of 6% from 1993 to 2007 (Prigent et al., 2012).

Modifications in up-stream land use, hydro-electric infrastructure, and increased water withdrawal, in conjunction with climate change, are considered to be the main factors modifying the flooding characteristics of wetlands. In particular, dam construction has altered many wetlands throughout Africa, such as those of the Senegal River Delta in Mauritania (Duvail and Hamerlynck, 2003) and in Senegal (Lamagat et al., 1996; Bader et al., 2003), the Inner Delta of the Niger River in Mali, the Waza Logone in Cameroon (Loth,
2004), the Medjerda River in North Africa (Zahar et al., 2008), the Tana River in Kenya (Maingi and Marsh, 2002) and the Hadejia-Jama‘are floodplains in Nigeria (Barbier and Thompson, 1998), while many others are threatened such as the Okavango Delta in Botswana (Milzow et al., 2009) and the Rufiji Delta (Duvail and Hamerlynck, 2007).

The flooding characteristics of wetlands, particularly the flood extent, timing, frequency, duration and flood peaks, largely determine the physical, chemical and biological properties of wetlands (Mitsch and Gosselink, 2000). Their quantification is therefore crucial for the management of wetlands and can be achieved through hydrological modelling.

Many types of flood models exist, ranging from lumped to distributed models. They mainly differ in their physical basis, complexity and data requirements. Distributed models are generally used when accurate data are available, while conceptual models are better suited to poorly gauged sites where data acquisition is difficult.

In recent years, there has been a rapid development of distributed models due to the proliferation of high-quality quantitative data (e.g. topography, remote-sensing imagery) and increasing computational power (Hunter et al., 2007). However, data, end-user and computational constraints also need to be considered (Beven and Freer, 2001). Furthermore, hydro-dynamic modelling of river-floodplain systems must be undertaken with precaution in large and flat floodplains, where small uncertainties in the water level can generate large errors in the prediction of flood extents.

For these reasons, more parsimonious approaches using simplified assumptions, have recently (re-)emerged in the scientific literature. In particular, lumped models combined with remote-sensing data have been used to characterize flood extents in poorly gauged and poorly characterized wetlands, such as the Okavango Delta (Wolski et al., 2006), and the Inner Delta of the Niger River (Mahe et al., 2011).

Remote sensing data can be used to detect water bodies and their characteristics (water extent, level, vegetation cover, sediment load, etc.) for calibration and validation of hydrological models. However, there are no standard methods to do so. Synthetic Aperture Radar imagery is very popular because of its high spatial resolution (e.g. a pixel size of 12.5 m for ERS-1 PRI data) and its capacity to map water under thick vegetation. However, the radar signals are sensitive to wind-induced waves, especially in the C-band, limiting the usefulness of this band for water detection (Alsdorf et al., 2007). L-band data are limited by their low orbital repeat cycles, cost and limited archives. Passive microwave data have been used to detect flood extents (Sippel et al., 1998; Ticehurst et al., 2009) but are also limited by a low spatial resolution. Thermal satellite data have been used to map inundated areas (LeBlanc et al., 2011), but to our knowledge, these data have an inadequate monthly timescale for characterizing rapidly changing flood extents. An alternative solution is the use of passive optical/infrared sensors on board the Landsat, Aqua, Terra or SPOT satellites.

The MODIS instruments on-board the Terra and Aqua satellites have been providing daily data for 36 spectral bands between 0.405 and 14.385 µm at a 250 m to 1 km resolution since 2000 and 2002, respectively. They have been used to characterize water levels (Ordoîne and Friedl, 2008), the seasonality of lake systems (Feng et al., 2012), the extent of annual flooding (Sakamoto et al., 2007) and to map wetlands and flooding patterns (Ticehurst et al., 2009; Islam et al., 2010). MYD09A1 is a level-3 high-quality composite product, with a 500 m resolution. Each pixel contains the best possible observation during an 8-day period, corrected for atmospheric gases and aerosols, and is hence useful in zones subject to high cloud cover. Furthermore, two bands describe the quality of each pixel regarding aerosols and the presence of clouds or cloud shadow so that masking poor quality pixels is possible. Despite their moderate resolution, the long-term data collection and frequent overpasses make this product a good candidate for monitoring large- to medium-sized wetland complexes.

The objective of this study was to quantify the main water fluxes and flooding characteristics in a poorly gauged East African wetland, the Tana River Delta (TRD). To do so, we constructed a lumped hydrological model (the Tana Inundation Model, TIM) that allowed us to determine the role of river fluxes in flooding events and the number of flood events from 2002 to 2011 and to characterize the extent and duration of these floods. Satellite data were used to calibrate and validate the model, and to provide a spatial representation of the flooded zones. The hydrological variables quantified in this study are relevant for the management of the wetlands. After a description of the TRD, focusing in particular on its hydrological characteristics, the MODIS satellite data are analyzed, and the Tana Inundation Model is presented. Finally, the results are described in detail and then discussed in the light of wetland management issues.

2 The Tana River Delta, Kenya

2.1 Socio-economic and environmental context

The Tana River Delta (TRD, Fig. 1) is located on the Kenyan coast between the towns of Garsen, Lamu and Malindi and extends roughly over 1300 km². The region is among the poorest in Kenya and its indicators of human well-being are extremely low (United Nations Development Programme, 2010). The local population (over 100 000 inhabitants) is predominantly from the Pokomo, Orma, Somali, Wardei and Wata communities (Republic of Kenya, 2010), and they mainly rely on farming, fishing and livestock-keeping activities for their subsistence (Leauthaud, 2009; Duvail et al., 2012; Leauthaud et al., 2013). In addition to the economic and human value of the TRD, its complex landscape mosaic has an exceptional biodiversity value (Hamerlynck et al., 2012).
Over the past fifty years, five major reservoirs have been built in the upper basin that have significantly modified the hydrological regime of the river, with a 20 % decrease in the peak flows of May (Maingi and Marsh, 2002). Other projects, particularly those of the Grand Falls Dam, could further impact the downstream flooding processes in the near future. In recent years, many biofuel and large irrigation schemes have also been initiated that will deprive the local communities of essential land and water resources (Duvail et al., 2012). It is therefore important to quantify current river water resources within the delta.

### 2.2 Basin characteristics and data constraints for hydrological modelling

The Tana is the largest river in Kenya and flows over nearly 1000 km from Mount Kenya and the Aberdare Mountains to the Indian Ocean. Its flowing pattern is bi-modal, with peak flows occurring during the long and short rainy seasons. Long-term discharge data were available at three locations within the Lower Tana Catchment. The closest long-term and active gauging station is at Garissa (0°27’49.19” S, 39°38’11.77” E, 1941–current), which is located 250 km upstream of the TRD. Two other gauging stations were located at Hola (1°30’00.00” S, 40°02’00.17” E, 1949–1991) and Garsen (2°16’09.36” S, 40°07’16.32” E, 1950–1998); however they are no longer monitored, and their data are discontinuous (22.8 and 41.2 % of gaps in record, respectively). Maximum peak discharges in Garissa were 1622 m$^3$s$^{-1}$ in 1941 and then 1585 m$^3$s$^{-1}$ in 1961.

Maingi and Marsh (2002) consider flood propagation and losses due to evaporation to be the major hydrological processes that occur within the semi-arid stretch between Garissa and Garsen. This consideration is supported by three facts:

1. a rapid analysis of river discharges at Garissa and Garsen shows that peak discharge rates are largely attenuated and smoothed out between the two stations (Fig. 2), with an average decrease in transiting volume of 76% (Table 1);

2. only seasonal rivers, such as Laga Tula, the Laga Galole and the Laga Tiva, flow into the Tana River within this stretch;

3. with a hypothetical water requirement of 2 L s$^{-1}$ ha$^{-1}$ and a cultivated area of 4000 ha, water abstraction at the Bura and TDIP irrigation schemes would not significantly alter the Tana River discharge during peak flows and hence the flooding characteristics in the TRD.

The precipitation decreases from the coast at Malindi (1098 ± 306 mm yr$^{-1}$, 1962–2008) to the inlands (530 ± 202 mm yr$^{-1}$) in Garsen, 1972–1986, data from the Kenya Meteorological Department, KMD, Kenya. Years with over one month of missing data were excluded. The rainfall pattern is bi-modal, with two rainy seasons extending from April to June and from November to December, both of which correspond to the flooding periods for the Tana River in natural conditions. Recent daily precipitation and minimum and maximum daily air temperatures for the...
Table 1. Mean water flow per season (and 1 standard deviation) at each station and the resulting water volume ratio between the stations. The number of seasons (Nb) used and the periods considered for each calculation are specified. Each year was divided into two hydrological seasons (1 March–31 August and 1 September–29 February) to better use the available data. Seasons with more than 20% of missing data were excluded (10 seasons for Garissa for 1941–2009; 60 for Garsen for 1951–1998). The remaining missing data, 2.3% (542 days) and 6.0% (397 days) for Garissa and Garsen, respectively, were filled in by linear interpolation.

<table>
<thead>
<tr>
<th>Station</th>
<th>Water flow</th>
<th>Nb</th>
<th>Period</th>
</tr>
</thead>
<tbody>
<tr>
<td>Garissa (km$^3$)</td>
<td>2.51 ± 1.34</td>
<td>115</td>
<td>1941–2009</td>
</tr>
<tr>
<td>Garsen (km$^3$)</td>
<td>1.56 ± 0.46</td>
<td>23</td>
<td>1951–1992</td>
</tr>
<tr>
<td>Volume ratio</td>
<td>0.76 ± 0.28</td>
<td>22</td>
<td>1951–1992</td>
</tr>
</tbody>
</table>

delta are also provided by the Tana Delta Irrigation Project (TDIP, 2°316′22.07″ S, 40°11′00.55″ E). Monthly precipitation data (from the KMD) are available from Garissa. Local precipitation most likely does not induce the floods but instead acts as a “wetting” event before the arrival of the flood wave. Precipitation is low in the semi-arid zones surrounding the delta. With an annual precipitation similar to that in Garissa (373 ± 202 mm yr$^{-1}$, 1962–2008; KMD) and a low topographical gradient, overland flow and regional groundwater flows to the floodplains are most likely limited, compared to the water brought by the Tana River.

The mean temperature in the delta (1998–2009, TDIP) is 28°C, with a mean maximum and minimum of 31°C in March and 26°C in July, respectively, suggesting high evaporation rates over the flooded areas, in accordance with regional monthly values (150–210 mm month$^{-1}$, Woodhead, 1968).

Within the delta itself, the main soil types encountered are deep, well drained, dark brown and cracking vertisols and fluvisols (Japan International Cooperation Agency, 1984a,b). The clayey nature of the floodplain soils most likely limits the infiltration of water within the floodplains during flood events. Ground water recharge could occur through infiltration at the sandier locations within the TRD, but quantitative data are unavailable.

Freely available digital elevation models (DEM), e.g. ASTER and SRTM, exist for the whole basin. However, the low resolution of these models relative to the measurements of the altitude makes them inappropriate for hydrological modelling in the flat floodplains of the TRD (the slope gradient from the delta inlet to the estuary is approximately 0.3%).

Finally, numerous satellite products (LANDSAT, SPOT, MODIS, radar products) are available at different spatial and

![Fig. 2. (a) Example of measured discharges at Garissa, $Q_1$, and Garsen, and simulated discharge at Garsen, $Q_2$, in 1988. (b) Simulated versus measured discharge at Garsen for the validation periods (1963–1986 and 1991–1998).](image-url)
temporal scales. However, a high cloud cover limits the use of many of those in the optical spectral range, while the overpass frequency of current radar products is too low to obtain a time series of flood extents.

The limited availability of hydrological, climate and topographical data makes the characterization of the flood events within the delta challenging. The rapid analysis of the discharge data suggests that downstream discharge rates can be reconstituted using those at Garissa but that peak discharge attenuation and delay time, as well as the decrease in the discharge rates, are important and hence need to be modelled. Within the delta itself, many water fluxes are ungauged while the DEMs are not precise enough to be used in hydrological studies. Therefore, a water balance model was used to quantify these fluxes, and the flood extents extracted from the medium temporal and spatial resolution remote-sensing products were used to calibrate the model in the absence of other data.

3 Approach: satellite data analysis and hydrological model specification

3.1 Strategy

To characterize flooded extents in the context of limited data, we constructed a tailor-made hydrological model, the Tana Inundation Model (TIM, Fig. 3). It first reconstitutes river discharge at the delta inlet and then performs a water balance within the delta, taking into account the main water fluxes (river discharges, rainfall, surface flow, evaporation and infiltration). In the absence of topographical data, a logistic equation related the water level within the delta with the flood extent. Calibrated parameters and their associated uncertainties were calculated by comparing these flood extents with those measured from the MODIS satellite data. The temporal dynamics of the floods in the TRD throughout the past decade were simulated with an estimation of the flood extent, duration and frequency. A yearly water balance was also calculated. Finally, the MODIS MYD09A1 products also generated a spatial representation of the flooded zones. The data used in this study are listed in Table 2, and each step of the analysis (Fig. 4) is further explained below.
3.2.1 Acquisition and pre-processing of images

The MYD09A1 500 m, 8-day composite images (tile H22V09) were downloaded from the NASA website (434 images from 4 July 2002 to 19 December 2011). All pixels with a high aerosol quantity or a MODIS cloud cover (indices extracted from the surface reflectance state quality layer) in the visual or mid-infrared bands (bands 2 and 5) were masked (LDOPE software tool, MODIS Land quality assessment group: Roy et al., 2002). The processed images were then reprojected into geographical coordinates, subset to the studied area (upper left corner: 2°6’0”S, 39°59’56.4”E, lower right corner: 2°6’0”S, 39°59’56.4”E) and transformed into geotiffs (HDF-EOS To GeoTIFF Conversion Tool, HEG v2.11, EOS, 2012).

Image analysis was carried out on the deltalic flood-plains, excluding the river mouth, mangroves and coastal forests. The geographical mask used was constructed manually through a visual interpretation of the 90 m Shuttle Radar Topography Mission Digital Elevation Model (SRTM DEM). Its contours roughly follow the Menjila-Lamu road to the north, the eastern and western terraces and the southern coastal forest and sand dunes (Fig. 1).

3.2.2 Detection of vegetated flooded pixels

Differences in the spectral signature of the land and water covers are used to distinguish the water bodies from the other surfaces. Many water indices have been developed using different spectral bands and different satellite data (Gao, 1996; McFeeters, 1996; Rogers and Kearney, 2004; Xu, 2006) and are commonly used to differentiate land cover types.

A major characteristic of the TRD is the frequent presence of a dense and low-lying vegetation cover above the water. Water indices do not always distinguish between the flooded and non-flooded vegetation. However, Oliesak (2008) used the Modified Normalized Difference Water Index (Xu, 2006) to map the open water bodies in the Inner Niger Delta and the Normalized Difference Water Index of Gao (NDWI$_{Gao,M2-5}$) (Gao, 1996) to include the vegetated water. Despite large differences in spatial extent between the Inner Niger Delta and the TRD, some main characteristics of the wetlands (flooded vegetation of Echinochloa stagnina (Retz) P. Beauv) are identical. We therefore used NDWI$_{Gao,M2-5}$ to map flood extents in the TRD.

\[
\text{NDWI}_{Gao,M2-5} = \frac{\rho_{\text{red}} - \rho_{\text{MIR}}}{\rho_{\text{red}} + \rho_{\text{MIR}}}
\]  

where $\rho_{\text{red}}$ and $\rho_{\text{MIR}}$ are the radiances (in reflectance units) in the red and mid-infrared spectral ranges, extracted from bands 2 (841–876 µm) and 5 (1230–1250 µm) of the MYD09A1 product.

To determine the index threshold that best differentiated between the flooded and dry areas, 1398 reference GPS points corresponding to 500 m by 500 m flooded or dry zones were manually acquired (Garmin eTrex Legend) on foot or by boat during two flood events (May 2010 and December 2011) and one rainy season when no floods occurred (May 2009) and were compared to the spatially and temporally coincident MYD09A1 pixels. These binary data
were used to construct error matrices for NDWI\textsubscript{Gao,M2-5} values ranging from 0.05 to 0.12 (at a step of 0.01). The NDWI\textsubscript{Gao,M2-5} value that maximized the percent of correctly classified pixels (i.e. the overall accuracy of Congalton, 1991) was retained as the threshold value. During the classification process, the misclassification of pixels in a flooded (resp. dry) state can be measured (the user’s accuracy of Congalton, 1991) and was used here to estimate an uncertainty range for the resulting flood extents, \( A_o \).

### 3.2.3 Classification of pixels and image analysis

Each pixel within the geographical mask was classified as flooded when its NDWI\textsubscript{Gao,M2-5} value was higher than this threshold value (and vice versa), or as clouded. The resulting MODIS imagery set was analyzed in three ways.

First, the empirical probability of flooded state, \( p_i \), for each pixel, \( i \), was calculated as

\[
p_i = \frac{n_{F,i}}{N_T - n_{c,i}}, \tag{2}
\]

where \( n_{F,i} \) is the number of times the pixel \( i \) was classified as flooded, \( N_T \) is the number of images available and \( n_{c,i} \) is the number of times that the pixel was classified as clouded at band 2 and band 5. This term expresses the fraction of times a pixel was classified in a flooded state, considering the observations of the pixel when it was classified as non-clouded. \( p_i \) was calculated for each pixel within the study site, and based on these calculations, we then drew an iso-contours map of \( p_i \).

Secondly, a discrete time series of flood extents was obtained from the images presenting less than 10% cloud cover for all seven bands. Flood extent \( A_o \) was calculated as

\[
A_o = \gamma \cdot n_F, \tag{3}
\]

where \( \gamma \) is the area of a MODIS pixel (0.216 km\(^2\)), and \( n_F \) is the number of pixels classified in a flooded state. Then, to obtain uncertainty boundaries, 1000 numerical simulations, following a random sampling with replacement design, were undertaken for each image and each of the three classes. The probabilities that each selected pixel had been correctly classified (in a flooded or dry state or in a flooded state but clouded) were taken, respectively, as the user’s accuracy for the flooded and dry classes from the error matrix and the ratio of pixels classified as flooded on pixels classified as non-clouded. The upper and lower uncertainty boundaries were then calculated as the 90th and 10th percentiles from the simulations centered around the previously calculated flooded area, so that a maximum \( A_{o,x} \) and minimum \( A_{o,m} \) flooded area were calculated for each image. Due to the non-random spatial distribution of the GPS data points, this method was only used to estimate the uncertainty range (for which the error is considered negligible as the cloud cover of the selected images was less than 10%) and not to calculate flood extents, for which a better estimate can be obtained from Eq. (3).

Lastly, the images were used to obtain an empirical probability of flood extent \( p \) using Eq. (3):

\[
p = \frac{n_S}{N_T} \tag{4}
\]

where \( n_S \) is the number of times the flood extent \( A_o \) was observed. To estimate \( A_o \), we considered that a zone subject to floods could be defined \( (p_i > 0.01) \), and that within this zone, clouds were randomly distributed so that the ratio of flooded to non-flooded area was identical to this same ratio in the clouded areas. Hence \( A_o \) was estimated as

\[
A_o = \gamma \cdot n_F \cdot \left( 1 + \frac{n_c}{n_T - n_c} \right), \tag{5}
\]

where \( n_c \) is number of pixels classified as clouded within the zone subject to floods and \( n_T \) is the number of pixels (2105 pixels) of the zone subject to floods within the studied zone (4789 pixels). In order to have a good estimation of the ratio, images where over 50% of the zone subject to floods was classified as clouded were excluded (96 images).

### 3.3 The Tana Inundation Model

#### 3.3.1 General structure

The Tana Inundation Model (TIM, Fig. 3) was composed of a non-linear flood routing model chained to a water balance model within the delta.

Input data were daily discharge rates at Garissa, \( Q_1 \) [L\(^3\) T\(^{-1}\)], daily precipitation at TDIP, \( R_D \) [L T\(^{-1}\)], monthly precipitation at Garissa, \( R_{SB} \) [L T\(^{-1}\)], and monthly potential evapotranspiration rates \( e \) [L T\(^{-1}\)] for the delta (Woodhead, 1968). Gaps in the \( Q_1 \) record were filled by linear interpolation, except for two periods when flood events occurred (5 May 2003–31 October 2003 and 31 March 2005–4 August 2005) for which this method is inappropriate. All results therefore exclude these periods. A 10-day moving average, which was more appropriate for the flood-routing model (Lamagat et al., 1993; Bader et al., 2003), was then used as the model input. State variables were daily discharge rates \( Q_2 \) at the delta inlet, daily discharge rates \( Q_3 \) at the delta outlet, daily evapotranspiration, infiltration and precipitation over the flooded area, \( E \), \( I \) and \( R \), daily overland flow \( L \) from the sub-basin between Garsen and the estuary, and daily flood extent \( A \) [L\(^2\)] within the delta. All fluxes are expressed in [L\(^3\) T\(^{-1}\)].

Once calibrated and validated, the model provided a time series of flood extents for 2002–2011, as well as the number of flood peaks, their mean duration and flood frequency. Finally, a mean yearly water balance for the delta provided estimations of main water inflows and outflows.

#### 3.3.2 Flow propagation within the river stretch

Discharge measurements, \( Q_2 \), were reconstructed using a flood routing model (Lamagat et al., 1993) that has been used
to model many large rivers with overflow in Africa (Lamagat et al., 1993; Bader et al., 2003; Belaud et al., 2010). This approach relies on a theoretical analysis of the diffusive wave equation and takes into account differences in propagation trends in low and high flow regimes.

According to this method, two empirical relationships were established between the upstream and downstream discharges ($Q_1$ and $Q_2$), and between the upstream station and a delay time, $T$. Calibration of the two empirical relations was performed with a subset of $Q_1$ and $Q_2$ discharge data (1 December 1986 to 29 June 1991). Upstream and downstream hydrographs were divided into 20 elementary intervals (Belaud et al., 2010), and then, a linear regression was performed between the discharge rates from the two stations for different delay times, $T$, and for each interval. The delay time $T$ was chosen to minimize the root mean square error (RMSE) of the linear regression, thus maximizing the correlation between $Q_1$ and $Q_2$. Due to scarce data, the empirical $Q_1 - Q_2$ relationship did not have the expected increasing trend at low discharges and was manually corrected. These relationships were then modelled with linear, second-order polynomial or logarithmic equations, by maximizing $R^2$ to obtain continuous functions relating $Q_1$, $Q_2$, and $T$. Discharge $Q_2$ was calculated as the resulting 10-day moving average daily discharge.

The Nash–Sutcliffe coefficient (NS), the absolute maximum error (AME), the RMSE, and the mean absolute error (MAE), as defined by Dawson (2007), were calculated for $Q_2$ for both the calibration (1986–1991) and validation (1963–1986 and 1991–1998) periods to assess the quality of the flood routing model.

### 3.3.3 Equations and specifications of the water balance model

The TRD was represented as a single reservoir, within which a daily water balance was calculated:

$$\frac{dV}{dt} = A \cdot \frac{dZ}{dt} = Q_2 + R + L - Q_3 - E - I \quad (6)$$

where $V$ [L$^3$], $Z$ [L] are the volume and the level of water within the reservoir.

In the absence of topographical data, the flooded area $A$ was related to water level $Z$ using a logistic equation:

$$A = \frac{A_{\text{max}}}{1 + a \cdot \exp^{-r \cdot Z}}, \quad (7)$$

where $A_{\text{max}}$ is the maximum flood extent, while $a$ [−] and $r$ [L$^{-1}$] determine the shape of the logistic curve.

Rainfall input, $R$, was calculated as

$$R = R_D \cdot A, \quad (8)$$

where $R_D$ is the daily precipitation at TDIP [L T$^{-1}$]. In the absence of daily precipitation data from 1 March 2007 to 31 December 2007, $R_D$ was uniformly distributed daily values calculated from the monthly precipitation data.

Overland flow, $L$, was calculated as a function of rainfall at Garissa, $R_{SB}$:

$$L = c_R \cdot R_{SB} \cdot (A_{SB} - A), \quad (9)$$

with $c_R$ being the runoff coefficient [−] and $A_{SB}$ [L$^2$] being the sub-basin area after Garsen (13 700 km$^2$). In the absence of daily precipitation data for the sub-basin, $R_{SB}$ was uniformly distributed daily values calculated from the monthly precipitation data at Garissa.

The outflow, $Q_3$, which is unknown in reality because of its diffuse character, was related to the level of the water stored above the reservoir's outlet at sea level, $Z_{SL}$ [L], in a classical manner, in other words:

$$Q_3 = \alpha \cdot (Z - Z_{SL})^\beta. \quad (10)$$

$Z - Z_{SL}$ represents the head loss between the reservoir and its outlet. $\alpha$ [L$^{3-\beta}$ T$^{-1}$] and $\beta$ [−] are the two parameters of the equation. The value of $\beta$ is typically between a minimum of 0.5 for a Chezy- or Manning-type flow and 1.5 for a free weir flow (Chow, 1959), which is what would be expected here.

Evaporation was calculated in the same way as Wolski et al. (2006):

$$E = e \cdot A. \quad (11)$$

In the absence of more precise data, uniformly distributed values of daily potential evapotranspiration, $e$ [L T$^{-1}$], were obtained from monthly estimates at Malindi (Woodhead, 1968).

Infiltration was expressed through a linear relationship relating it to the flooded area, $A$:

$$I = c_I \cdot A, \quad (12)$$

where $c_I$ is the infiltration rate [L T$^{-1}$].

The model was coded under R (R Development Core Team, 2008) and verified by checking the closure of the water balance for all parameter sets retained in the calibration process. The minimum flooded area $A_{\text{min}}$ was set to 1 km$^2$, and the maximal water level was set to 10 m to keep the reservoir shape conforming to the TRD. $a$ was calculated from Eq. (7) using the area of permanent lakes $A_L$ (4 km$^2$) and the three parameters $Z_L$, $A_{\text{max}}$ and $r$. Initial flood extent was set to $A_L$ because the model was initiated at low flow. When the flood extent was minimal, evapotranspiration and infiltration were considered to be negligible. Equation (6) was solved iteratively using the fourth-order Runge–Kutta algorithm (Atkinson, 1989). For reasons of numerical stability, it was solved at an hourly time step. Final output variables were averaged over 10 days so that the temporal resolution was close to that of the MODIS images and major input variables.
3.4 Calibration and validation strategy for the water balance model

Calibration and validation of hydrological models are usually performed by comparing the simulated data with an independent set of data. Classical evaluation metrics include NS, AME, MAE and RMSE (Table 4). The water balance model had eight parameters (Table 3), which were estimated according to the equifinality concept (Beven and Binley, 1992). This concept states that the uncertainty related to parameter estimations allows for multiple parameter sets to reproduce the observed behavior of a system. This uncertainty needs to be quantified in the modelling procedure (Beven and Binley, 1992) because it affects the interpretation of the model.

In this study, we were interested in (1) selecting parameter sets during a calibration process, then validating each set, and (2) assessing the final quality of the model, which includes the ensemble of parameter sets. In the first case, point simulations were to be compared to an uncertainty range issued from the MODIS images, whilst in the second case, two uncertainty ranges were to be compared. To do so, we defined an evaluation metric $L_e$ as

$$L_e = 1 - \frac{\sum \epsilon^2}{\sum (A_o - \bar{A}_o)^2}, \quad (13)$$

where $\epsilon$ (Fig. 5) is the error defined in Eq. (14) or Eq. (15), $A_o$ is the flooded area observed at each date and $\bar{A}_o$ is the mean flooded area from the MODIS images. The likelihood $L_e$ differs from the Nash–Sutcliffe coefficient because it compares flood extents rather than discharges and differs in the definition of the error $\epsilon$. The latter is the difference between the value measured by MODIS and that simulated by TIM, taking into account the uncertainty ranges. In the calibration and validation of each parameter set, $\epsilon$ was defined between the value from TIM and the uncertainty range from MODIS, so that

If $A < A_{o,m}$ then $\epsilon_1 = A_{o,m} - A$
If $A_{o,m} \leq A \leq A_{o,x}$ then $\epsilon_1 = 0$
If $A > A_{o,x}$ then $\epsilon_1 = A - A_{o,x}$. \quad (14)

In the quality assessment phase, $L_e$ was defined using not only the uncertainty range of the MODIS data, but also the uncertainty range of TIM as the equifinality concept states that all selected parameter sets are acceptable. Hence, $\epsilon$ becomes as follows:

If $A_{0,9} < A_{o,m}$ then $\epsilon_2 = A_{o,m} - A_{0,9}$
If $A_{o,m} \leq A_{0,9}$ and $A_{o,1} \leq A_{o,x}$ then $\epsilon_2 = 0$
If $A_{0,1} > A_{o,x}$ then $\epsilon_2 = A_{0,1} - A_{o,x}$. \quad (15)

where $A_{0,1}$ and $A_{0,9}$ are the 10th and 90th percentile boundaries for the calibrated hydrological model. The advantage of this approach is that it increases the flexibility in the calibration process for a model that needs to be constrained using a very limited amount of data.

Model calibration was performed using the Generalized Likelihood Uncertainty Estimation (GLUE) methodology (Beven and Binley, 1992; Beven and Freer, 2001). Ranges
were fixed for the model parameters (Table 3), and the parameter sets were randomly generated within these bounds, using a uniform distribution. The model was then run with each parameter set, and the results that did not meet our acceptance criteria were rejected. A first selection was conducted by retaining the sets yielding a $\mathcal{L}_e > 0.60$ and a full solution of the differential equation (Eq. 6). Secondly, the parameter sets were further restrained to reproduce the observed conditions (a flood extent higher than 150 km$^2$ on 31 May 2010 or lower than 10 km$^2$ in May 2009).

This parameter selection was performed using a split-sample approach. The time series was separated into two periods (1 January 2002–21 September 2006 and 22 September 2006–31 December 2011), each of which was used for the selection of a limited number of parameter sets. The initial pool consisted of 200 000 sets of parameters for each period. Finally, both reduced sets were combined, and the uncertainty ranges were defined by the 90th and 10th quartiles obtained from the likelihood-weighted output variables.

Each parameter set was validated by calculating the evaluation metrics ($\mathcal{L}_e$, $\mathrm{AME}_e$, $\mathrm{MAE}_e$, $\mathrm{RMSE}_e$, with the error defined from $\epsilon_1$) from the data not used during the calibration process. In the final assessment of the quality of the water balance model, including the ensemble of parameter sets, $\mathcal{L}_e$, $\mathrm{AME}_e$, $\mathrm{MAE}_e$, $\mathrm{RMSE}_e$ were calculated for 2002–2011, with the error defined from $\epsilon_2$.

### 4 Results

#### 4.1 Satellite data

The overall accuracy of the pixel classification was maximal (92.63%) at NDWI$_{Gao,M2.5}$ = 0.09 (Table 5). The overall accuracy always exceeded 85% for all the NDWI$_{Gao,M2.5}$ values between 0.05 and 0.012, showing that the index was not sensitive within this range.

Seventy-six images (Fig. 6) were characterized by a cloud cover of less than 10%. The resulting set was well-distributed between the rainy and dry seasons. The maximum and minimum flood extents were 0–6 km$^2$ and 302–316 km$^2$ (10th and 90th percentiles). Only 19 images presented a flood extent over 100 km$^2$.

### Table 3. Definition of water balance model parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Signification</th>
<th>Range/value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha$</td>
<td>parameter for discharge $Q_3$</td>
<td>0–10E6</td>
<td>m$^3$·day$^{-1}$</td>
</tr>
<tr>
<td>$\beta$</td>
<td>parameter for discharge $Q_3$</td>
<td>0.2–1.7</td>
<td>–</td>
</tr>
<tr>
<td>$A_{\text{max}}$</td>
<td>maximum flooded area</td>
<td>300–700</td>
<td>km$^2$</td>
</tr>
<tr>
<td>$r$</td>
<td>parameter for logistic equation</td>
<td>1–40</td>
<td>m$^{-1}$</td>
</tr>
<tr>
<td>$c_R$</td>
<td>overland runoff coefficient</td>
<td>0–0.05</td>
<td>–</td>
</tr>
<tr>
<td>$c_l$</td>
<td>infiltration rate</td>
<td>0–25$^*$</td>
<td>mm day$^{-1}$</td>
</tr>
<tr>
<td>$Z_L$</td>
<td>water level of permanent lakes</td>
<td>0–2</td>
<td>m</td>
</tr>
<tr>
<td>$Z_{SL}$</td>
<td>water level at outlet</td>
<td>0–5</td>
<td>m</td>
</tr>
</tbody>
</table>

* Parameter range from Clapp and Hornberger (1978).

#### 4.2 TIM

##### 4.2.1 Calibration and validation of the flood-routing model

The model reproduces the observed discharges at the Garsen station to a satisfactory degree, with reasonable NS, RMSE, $\mathrm{AME}$ and $\mathrm{MAE}$ for both the calibration and validation periods (Table 6).

The discharge at Garsen ($Q_2$, m$^3$·s$^{-1}$) and the time delay ($T$, day) are described by Eqs. (16) and (17):

If $Q_1 \in [0, 320]$ then $Q_2(t) = -0.0014 \cdot Q_1^2(t - T) + 0.9557 \cdot Q_1(t - T)$ + 145.69

If $Q_1 > 320$ then $Q_2(t) = 0.04692 \cdot Q_1(t - T) + 145.69$ (16)

If $Q_1 \in [0, 36]$ then $T = 5$

If $Q_1 \in [36, 78]$ then $T = 0.0033 \cdot Q_1^2 - 0.3715 \cdot Q_1 + 14.256$

If $Q_1 > 78$ then $T = 3.5588 \cdot \ln (Q_1) - 10.085$. (17)

The resulting curves are typical of an overflowing river with a very low slope. Downstream discharge increased with
Fig. 6. Flood extent in the delta for 2002–2011, as computed by TIM or measured from the MODIS imagery.

Fig. 7. Map of the iso-contours of empirical probability of flooded state, extracted from the MODIS images (2002–2011).
upstream discharge. At high discharges, the slope of Eq. (16) decreased due to overflowing into the floodplains and the consequent evaporation. At high discharges, \( Q_1 \), time-delay \( T \) increased as water overflowed into the large floodplains. According to the model, a flood of 500 m\(^3\) s\(^{-1}\) required approximately 12 days to reach Garsen from Garissa.

### 4.2.2 Calibration and validation of the water balance model

Calibrated parameters are presented in Table 3. They did not reveal any structure within the prior distribution space. However, \( Z_L \) and \( Z_{SL} \) were highly correlated (0.84), \( r \) and \( \alpha \) showed a correlation of 0.44, and \( \alpha \) and \( \beta \) showed a correlation of 0.37. The correlations (absolute values) between the other parameters were all less than 0.24 (and mostly less than 0.1). The correlation between \( Z_L \) and \( Z_{SL} \) was high because the water level within the delta is always higher than that at the outlet.

During the 2002–2006 calibration period, 462 sets of parameters were selected using the GLUE approach (Table 7). The likelihood, \( L_\epsilon \), was of 0.91 and 0.83 for the calibration and validation periods. During the 2006–2011 calibration period, 72 sets of parameters were selected (Table 7). \( L_\epsilon \) was 0.73 and 0.89 for the calibration and validation periods, respectively. The model seems better adapted to the 2002–2006 period, which has more parameter sets and higher \( L_\epsilon \) values compared to 2006–2011. After further restriction, 112 parameter sets were finally retained. The global model performance for each period and the entire 2002–2011 period are summarized in Table 7. \( L_\epsilon \), \( AME_\epsilon \) and \( MAE_\epsilon \) were, respectively, 0.93, 102 km\(^2\) and 9 km\(^2\) for the entire period. In light of these criteria, the proposed model performed well.

Finally, a water balance for each selected parameter set was computed. The median total volume of water transiting through the system was 28.9 ± 0.5 km\(^3\). A mean absolute difference of 0.86 % between the incoming and outgoing fluxes for all of the parameter sets was observed and attributed to the approximations of the numerical resolution. This difference is considered negligible.

### 4.3 Quantification of hydrological variables

Flood extents simulated by TIM for 2002–2011 are represented in Fig. 6. They corroborated well with the flood extents calculated from the MODIS imagery. The periodicity of the floods was well reproduced, with floods occurring during the rainy seasons. According to the hydrological model, the maximum flood peaks of the past decade occurred in May and December 2002, with median and 90th percentile values of 304 and 383 km\(^2\), and 272 and 385 km\(^2\), respectively. On the contrary, the floods of May 2011 seem to have been negligible ( < 100 km\(^2\)). The last fact was confirmed in the field.
Table 8. Number of floods and their mean duration (days) for 2002–2011.

<table>
<thead>
<tr>
<th>Flood extent</th>
<th>10th percentile</th>
<th>Median</th>
<th>90th percentile</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Nb Duration</td>
<td>Nb</td>
<td>Nb Duration</td>
</tr>
<tr>
<td>&gt; 100 km²</td>
<td>17 27 ± 19</td>
<td>16 43 ± 25</td>
<td>17 50 ± 25</td>
</tr>
<tr>
<td>&gt; 200 km²</td>
<td>5 11 ± 4</td>
<td>9 18 ± 11</td>
<td>15 28 ± 20</td>
</tr>
<tr>
<td>&gt; 300 km²</td>
<td>0 0</td>
<td>1 6</td>
<td>5 19 ± 6</td>
</tr>
</tbody>
</table>

Fig. 8. Histogram of flood extents calculated from the TIM and MODIS images. Counts were conducted every eight days. Total numbers of counts were 413 and 338 for TIM and MODIS, respectively.

Sixteen flood events with flood peaks over 100 km² (median value) were recorded for 2002–2011 (Table 8). Their duration was 43 days (median value). Among these floods, four lasted less than 20 days. These events were quite regular, with floods over 100 km² lasting more than 20 days occurring for over 2/3 of the rainy seasons. However, because of the calibration procedure of TIM, small flood extents could be overestimated.

Flood events of a larger scale were more rare, with a median number of nine flood events over 200 km² for the 18 recorded potential flooding periods. These floods occurred on average once a year, even though there are two potential flooding seasons per year. Their mean median and 90th percentile durations were 18 ± 11 days and 28 ± 20 days, respectively, with the longest 90th percentile flood durations of 45 and 82 days having taken place in May 2002 and December 2007, respectively. Flood events over 300 km² were recorded 0 to 3 times and were of short duration.

Table 9. Annual water flows (km³ yr⁻¹), calculated from the median values of TIM.

<table>
<thead>
<tr>
<th>Flow</th>
<th>2002–2011¹</th>
<th>2009²</th>
<th>2007³</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total discharge Q₂</td>
<td>3.17</td>
<td>2.54</td>
<td>3.90</td>
</tr>
<tr>
<td>Total rainfall R</td>
<td>0.06</td>
<td>0.04</td>
<td>0.10</td>
</tr>
<tr>
<td>Total overland flow L</td>
<td>0.09</td>
<td>0.08</td>
<td>0.09</td>
</tr>
<tr>
<td>Total inflow (Q₂ + R + L)</td>
<td>3.32</td>
<td>2.66</td>
<td>4.09</td>
</tr>
<tr>
<td>Total discharge Q₃</td>
<td>2.95</td>
<td>2.53</td>
<td>3.49</td>
</tr>
<tr>
<td>Total evapotranspiration E</td>
<td>0.11</td>
<td>0.04</td>
<td>0.20</td>
</tr>
<tr>
<td>Total infiltration I</td>
<td>0.22</td>
<td>0.09</td>
<td>0.39</td>
</tr>
<tr>
<td>Total outflow (Q₃ + E + I)</td>
<td>3.28</td>
<td>2.66</td>
<td>4.08</td>
</tr>
</tbody>
</table>

¹ mean; ² minimum value; ³ maximum value.

For the whole 2002–2011 period, flood extent was lower than 10 km² 48 % of the time (Fig. 8) while flood extents over 100 and 200 km² were observed 22 and 4 % of the time. These results corroborate with the empirical probability of flood extent calculated from the MODIS imagery (Fig. 8).

An empirical relationship relating the flood extent A with the incoming discharge Q₂ was also obtained from the TIM (Fig. 9). Confidence intervals (median values of the 10th and 90th percentiles of each data point) were calculated. Only three floods corresponding to extreme rainfall events do not fall within these intervals. Floods exceeding 100 km² occurred for discharges higher than 130 m³ s⁻¹ (median value of the 90th percentile of each data point). An increase of 30 m³ s⁻¹ resulted in floods of nearly 200 km².

Finally, the annual water balances were calculated for 2002–2011 using the median values of the parameter ensemble (Table 9). The total input discharge, rainfall, overland flow, output discharge, evapotranspiration and infiltration flows calculated in the water balance are represented in Fig. 10. Mean annual water inflow into the delta was approximately 3.3 km³ yr⁻¹. The minimum and maximum yearly inflows were observed in 2009 and 2007 at 2.7 and 4.1 km³ yr⁻¹, respectively. The river discharges Q₂ and Q₃ corresponded to over 95 and 89 %, respectively, of the mean annual water inflow.

5 Discussion and conclusions

5.1 Remotely sensed detection of flood extents

The NDWI_Gao,M2-5 index properly distinguished the flooded surfaces, including the low-lying vegetated flooded zones, from dry surfaces. Furthermore, this index can be calculated from many of the MODIS products, as well as from other optical sensors, such as LANDSAT, making it a good candidate to monitor flooded surfaces with a low-lying vegetated cover, which is typically found in wetlands.
The use of the MYD09A1 composite product from the MODIS instruments allowed the characterization of the state of the surface despite a high cloud cover. In particular, it gave the first estimation of the spatial flooding pattern and a time series of flood extents, that are in good agreement with the water balance model. The use of finer-resolution satellite products would improve the estimation of flooded area by decreasing the classification error due to mixed pixels. However, the disadvantages concerning its medium spatial resolution and 8-day uncertainty range are counter-balanced by its availability and high temporal resolution compared to many other satellite products. It can therefore be used in combination with the latter to characterize and monitor floods in medium- to large-scale wetland complexes.

5.2 The Tana Inundation Model

The use of a lumped model in combination with satellite data is a first step in quantifying the flooding characteristics in the poorly gauged wetlands of the Tana River Delta. By doing so, this paper contributes to the growing literature on the use of hydrological modelling in ungauged basins and follows previous recommendations to use “tailor-made” and “site-specific” models (Savenije, 2009).

The water balance approach adopted here was relevant to study the TRD system, for which information on the internal properties and processes were limited. The downscaling of rainfall and evaporation from monthly to daily data was justified as these flows account for only a small part of the water balance. The global fluxes generating floods and the flooding characteristics in the deltaic floodplains were quantified. These results have relatively high uncertainty ranges linked to the lack of essential data, such as a Digital Elevation Model and the scarcity of recent discharge measurements within the delta. Moreover, because of the chosen evaluation metric, the relative uncertainty for the low inundation extents is larger than for the high values. The model should therefore be better at capturing large flooded areas. Finally, the annual water balance confirms that the river discharge coming from Garissa, and therefore the upper basin, is the major process controlling the flooding events within the Tana River Delta.

In the future, semi-distributed or distributed models could be developed for the TRD. This study helps define which data are essential but unavailable in the zone, so that future research efforts concentrate on the acquisition of such data. Regular discharge or water level measurements at the inlet, outlet and other strategic locations (channel bifurcations, etc.) should be undertaken. A precise topographic map is necessary to describe the volume-area-water level relationships and hence the channel-overland flow dynamics. Lastly, in-situ or satellite measurements of flood extents are essential for parameter estimation and validation of future models.

5.3 Management issues

This study determined the major characteristics of flood propagation within the Garissa–Garsen stretch. An understanding of these characteristics is essential for the management of water resources. These characteristics seem to have remained identical throughout 1963–2011, despite the construction of five dams. This finding is particularly interesting in the context of hydroelectric infrastructure development because it supports the idea that dams could have modified the volume of transiting water (Maingi and Marsh, 2002) but not the flood propagation characteristics.

TIM provides an ensemble of flooding characteristics (flood extent, duration, timing, frequency of occurrence) that are essential in flood forecasting. The discharge–flood extent relationship also enables a rapid estimation of flood extents, which is information that can be used to monitor or predict floods in the delta. The MODIS images give complementary information concerning the spatial flooding patterns, which are also crucial for wetland monitoring. These images could be used to define the current flood-prone zones. Finally, this study highlights the idea that river fluxes are the main generator of floods within the delta. This result is important in the current context of hydroelectric infrastructure development on the Tana River.

Together, the results and the model developed in the study can help predict the consequences of the modification of the hydrological regime of the river on flooding events in the delta. Such prediction is essential because many ecosystems
Fig. 10. Simulated total daily discharges $Q_2$, $Q_3$, rainfall $R$, overland flow $L$, evapotranspiration $E$, and infiltration $I$ for 2002–2011, as computed by TIM.

and local communities are dependent on the dynamic flooding regime of the Tana River.

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