Monthly hydrometeorological ensemble prediction of streamflow
droughts and corresponding drought indices

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Abstract. Streamflow droughts, characterized by low runoff
as consequence of a drought event, affect numerous aspects
of life. Economic sectors that are impacted by low stream-
flow are, e.g., power production, agriculture, tourism, water
quality management and shipping. Those sectors could po-
tentially benefit from forecasts of streamflow drought events,
even of short events on the monthly time scales or below. Nu-
umerical hydrometeorological models have increasingly been
used to forecast low streamflow and have become the focus
of recent research. Here, we consider daily ensemble runoff
forecasts for the river Thur, which has its source in the Swiss
Alps. We focus on the evaluation of low streamflow and
of the derived indices as duration, severity and magnitude,
characterizing streamflow droughts up to a lead time of one
month.

The ECMWF VarEPS 5-member ensemble reforecast,
which covers 18 yr, is used as forcing for the hydrologi-
cal model PREVAH. A thorough verification reveals that,
compared to probabilistic peak-flow forecasts, which show
skill up to a lead time of two weeks, forecasts of stream-
flow droughts are skilful over the entire forecast range of one
month. For forecasts at the lower end of the runoff regime,
the quality of the initial state seems to be crucial to achieve a
good forecast quality in the longer range. It is shown that the
states used in this study to initialize forecasts satisfy this re-
quirement. The produced forecasts of streamflow drought in-
dices, derived from the ensemble forecasts, could be benefi-
cially included in a decision-making process. This is valid for
probabilistic forecasts of streamflow drought events falling
below a daily varying threshold, based on a quantile derived
from a runoff climatology. Although the forecasts have a ten-
dency to overpredict streamflow droughts, it is shown that the
relative economic value of the ensemble forecasts reaches up
to 60 %, in case a forecast user is able to take preventive ac-
tion based on the forecast.

1 Introduction

Droughts, which can occur on a wide spatial and temporal
range, can be defined in various ways. Typical and possibly
interrelated processes are a temporally and spatially extended
lack of precipitation (meteorological droughts), reduced soil
moisture (agricultural droughts) and low levels of runoff or
groundwater (hydrological droughts) (Heim Jr., 2002). This
variety in the way droughts are defined is a direct conse-
quence of the range of socioeconomic impacts they have on
different interest groups. It is common to study the char-
acteristics of low streamflow-related droughts on seasonal
time scales (e.g., (Vidal et al., 2010)). However, streamflow
droughts also appear on shorter time scales (Tallaksen et al.,
1997). Some of the short, consecutive events might be con-
nected to one prolonged drought; nevertheless they can cause
damage to certain susceptible sectors and are worthwhile to
consider individually. Streamflow drought forecasts on time
scales up to one month are potentially useful for hydro-power
generation, agriculture (irrigation), conventional power pro-
duction (supply of heat exchange water), water quality, nav-
igation (shipping) and tourism (e.g., water supply for snow
cannons), in general, all sectors that can use the information
about upcoming streamflow drought events to take preven-
tive action. For those sectors, skillful forecasts of streamflow
droughts could help to prevent or mitigate the consequences
of a water shortage (Steinemann, 2006).
Generally, two approaches to predict properties of low streamflow events in the long range can be discerned. First, stochastic approaches that relate the current state of a catchment and potential predictors to what has been observed in the past, to infer the likelihood of low streamflow within the prediction period. These include regression techniques (Morr eira et al., 2008; Cebrián and Abaurrea, 2011; van Og trop et al., 2011), time series models (Lohani and Loganathan, 1997; Ch ung and Salas, 2000; Mishra and Desai, 2005; Bordi and Sutera, 2007), and neural network techniques (Kim and Valdés, 2003; Mishra and Desai, 2006; Morid et al., 2007). Also procedures identifying correlations of drought events with teleconnection patterns (Tadesse et al., 2005; Özger et al., 2012) or certain weather types (Fleig et al., 2011) can be used to indicate potential drought events. Cancelliere et al. (2006) and Hwang and Carbone (2009) used autoregressive models not only to predict drought indices but additionally to quantify the uncertainty of their prediction. Drought indices inferred from statistically downscaled atmospheric models (Cacciamani et al., 2007) also have proven predictive quality.

The second, less common approach for the long-range prediction of droughts involves a coupled atmospheric–hydrological model. Wood et al. (2002) employ monthly forecasts from a global atmospheric model to drive a grid-based hydrological model that produces reasonable predictions of low streamflow up to several months in advance. The refined systems of Li et al. (2008) and Luo and Wood (2007) were able to predict average monthly drought conditions up to three months ahead.

In this study, we assess the quality of forecasts of hydrological droughts, characterized by low streamflow, for a lead time of up to one month. Streamflow is an appealing measure for droughts as it combines different catchment aspects, ranging from the input of precipitation to storage and transfer processes. By coupling or forcing hydrological with meteorological models, useful peak-flow predictions for a shorter forecast range are possible. As the predictability of an event mainly depends on its lifetime (Hirschberg et al., 2011), peak-flow forecasts rarely show skill beyond 10 days. This, however, depends on the catchment characteristics, as well as the quality of the models involved and the observations needed for an appropriate initialization (Webster et al., 2010; Fundel and Zappa, 2011). Streamflow droughts on the other hand are generally rather persistent phenomena. This is why predictions could potentially still be valuable in the longer range. It might therefore be worthwhile investigating their properties at lead times long after peak-flow predictions have lost their value. The value of forecasts can be increased if additionally the prediction uncertainty is quantified, e.g., by using a meteorological ensemble prediction system (EPS) or a multi-model ensemble (Cloke and Pappenberger, 2009) or multiple hydrological models maybe applying different model parameterizations (Rings et al., 2012).

This study introduces several new aspects of forecasting streamflow droughts such as, compared to existing studies on streamflow drought, a high temporal resolution and an ensemble approach to include forecast uncertainty. Daily predictions of streamflow drought up to a lead time of one month, employing the VarEPS ensemble reforecast (Vitart et al., 2008b) from the European Centre for Medium-Range Weather Forecast (ECMWF) as forcing for the hydrological model PREVAH (Viviroli et al., 2009), are assessed. Compared to the above-mentioned studies on the prediction of hydrological droughts, a higher temporal resolution is examined. The daily mean catchment runoff forecasts of 32-day lead time were produced in the period from 1991–2008, providing a large sample size and hence a robust estimation of forecast value. A further new aspect is the evaluation of forecasts regarding the lower end of the flow regime by considering indices describing low streamflow scenarios, namely duration, severity and magnitude. Below normal levels of streamflow can have socioeconomic impacts at all times of the year, also in seasons that are generally not associated with water shortages. To address this, a daily varying threshold based on past observations of streamflow is used to indicate streamflow droughts. Compared to monthly average forecasts of drought indicators, the here considered forecasts could be potentially useful for a new group of users, especially forecast users that are affected by short events and users that can take preventive action having a relatively short warning lead time. To estimate the value for a variety of users, the resulting forecasts are evaluated in terms of their economic value.

2 Data and methodology

2.1 Domain

The domain chosen for this study is the pre-alpine catchment of the Thur River located in the north-eastern part of Switzerland. The Thur River has a length of 127 km and discharges into the Rhine River. The catchment is 1696 km² in area, and its vertical extent is from 356 at the gauging station in Andelfingen to 2503 m a.s.l. at the top of the Säntis. The mean altitude is 769 m a.s.l.; 25 % of the catchment lies above 1000 m a.s.l and 0.6 % above 2000 m a.s.l. The submontane climate is relatively cool, and the runoff-generating processes from autumn to spring are affected by snowfall and melt processes. The annual average precipitation amount is about 1500 mm and mainly falls during the summer months. Figure 1 shows the monthly catchment average temperature mean and precipitation sum in the study period 1991–2008. Due to the vertical extension of the catchment topography, the values can differ largely within the catchment. Average values of other meteorological variables and their height distributions are given in Gurz et al. (1999). Figure 2 (left) shows some lower quantiles of catchment runoff, measured at the gauging station in Andelfingen from 1991–2008 using a sliding window of 31 days centered on the date of
interest. The maximum of runoff in April can be attributed to snowmelt. The runoff minima from September to February, depending on the considered quantile, are caused by the combination of less precipitation and snow accumulation.

This catchment, which is relatively large for Alpine conditions, was chosen as in smaller catchments streamflow drought rarely occurs over a longer period. In small catchments, low streamflow events are easily interrupted by small-scale precipitation events, which complicates the evaluation of longer-lasting events. A large catchment is therefore thought to be more appropriate to demonstrate the forecast value for longer events happening within the range of one month. Besides that, the runoff regime is relatively unaffected by human influences; i.e., no reservoirs or weirs are installed (Gurtz et al., 1999) that could potentially alter the runoff during periods of low streamflow.

2.2 Meteorological forcing

The unified variable resolution ensemble prediction system VarEPS (Vitart et al., 2008a,b) operated by the ECMWF produces each week a global, 51-member forecast with a lead time of 32 days. Its horizontal resolution is 50 km for the first 10 days and 80 km in the remaining 11–32 days. From day 10 onwards, the atmospheric model is coupled to an oceanic model. The motivation for varying the resolution is to benefit from the higher resolution in the early forecast range at longer lead times. At the time of this study, the forecasts were issued for Thursday at 00:00 UTC and were archived in time-steps of 6 h.

With each run of the operational VarEPS, an ensemble reforecast is started for the same day of the year over the past 18 yr, and also ranges over 32 days. The reforecasts share the same model version as the forecasts and are meant to capture the same model errors, e.g., to allow for an efficient post-processing, a more robust evaluation of forecast skill and a more target-oriented model development. The VarEPS reforecast dataset consists of 954 (18 yr × 53 initializations per year) ensemble forecasts. Unlike the operational forecast, the reforecasts have 5 ensemble members only, initialized with states taken from the ECMWF global reanalysis ERA-Interim or from ERA40. More detailed information about the history of model developments is available at http://www.ecmwf.int/products/data/technical/model_id/index.html.

For this study the VarEPS 5-member reforecast is used to drive the hydrological model. Fields of wind speed, 2 m temperature, 2 m dew point, sunshine duration, surface albedo and solar radiation are required as input. To meet the grid size of the hydrological model of 500 m × 500 m, a downscaling was performed, based on a bilinear interpolation (Gurtz et al., 1999; Viviroli and Gurtz, 2007). Temperature was adjusted according to elevation, assuming a lapse rate of 0.65 °C/100 m (Jaun and Ahrens, 2009).

2.3 Hydrological model

Runoff predictions were generated using the semi-distributed hydrological model Precipitation Runoff EVApotranspiration Hydrotope (PREVAH, Viviroli et al., 2009), with VarEPS as the meteorological forcing. PREVAH consists of hydrological response units (HRUs) and a runoff generation module based on the HBV model (Bergström and Forsman, 1973), taking account of the spatial distribution. Information on PREVAH physics and the parameterization is given in Gurtz et al. (1999) and Viviroli and Gurtz (2007). PREVAH’s parameter setting was conditioned by matching the produced runoff to observed runoff at the gauging station in Andelfingen for the period from 1995–2000. This optimization was performed with a focus on the average flow volume. PREVAH runs in hourly time steps. For this study, however, only daily mean runoff is considered. The setup of PREVAH adopted for the Thur basin is the same as the one used in Fundel and Zappa (2011) and Zappa and Kan (2007). In the latter publications the calibration and verification of the modeled runoff against the observed runoff, the water balance components, and hydrographs are presented.

Initial conditions for each forecast run were obtained from a continuous reference simulation forced with meteorological surface observations from 12 measurement sites, 6 within and 6 outside a distance of 100 km to catchment. The initial states contain information about the water storage in the different modules of each HRU. To highlight the quality of the initial conditions, Fig. 2 shows a comparison of the reference simulation and the runoff observed at the gauging station in Andelfingen for the low runoff regime. The seasonal cycle and the runoff volume concur well. The evaluation of daily mean runoff from the reference simulation during the study period 1991–2008 results in a mean error of –0.003 mm h⁻¹ (−3 %), a Nash–Sutcliffe coefficient (Nash and Sutcliffe, 1970) of 0.87 respectively 0.88 using logarithmized runoff.

When investigating forecasts of observations of hydrological droughts, a smoothing or pooling algorithm, spanning
several days, is often applied to the data in order to avoid counting several short events that belong to the same large-scale drought. Here, however, no further smoothing of the daily forecasts is applied, mainly in order to evaluate the predictive capability of the hydrometeorological prediction system that has the potential to simulate short-term variability in runoff but also due to the fact that shorter events of abnormally low streamflow can lead to economic losses as well.

### 2.4 Characterization of hydrological droughts

Streamflow droughts are generally characterized by the indices duration (time between onset and offset), severity (cumulative water deficit) and magnitude (severity/duration) (Tallaksen et al., 1997; Hisdal and Tallaksen, 2000; Hisdal et al., 2001; Smakhtin, 2001; Zaidman et al., 2002; Fleig et al., 2006; Nalbantis and Tsakiris, 2008; Mishra and Singh, 2010; Yoo et al., 2011). Defining hydrological droughts solely by considering those indices requires the assignment of a runoff threshold. Whenever the predicted or observed runoff falls below that threshold, this counts as an event of streamflow drought. Figure 3 illustrates the streamflow drought indices drawn from an observed or forecast hydrograph, with indices being dependent on the choice of the threshold. It is, however, not obvious where the threshold should be set. Some stakeholders sensitive to low streamflow may be interested in a constant threshold, e.g., a power plant that requires a certain amount of water for cooling. Others might be affected by droughts only in certain seasons, e.g., tourism. To meet both concerns, a variable, quantile-based streamflow drought threshold was selected. The threshold was calculated individually for each day of the year, using runoff from the 18-yr study period and a gliding 31-day window around the date of interest. This implicates that events associated with higher runoff, which would not be considered as streamflow drought events in other, drier parts of the year. However, in this study streamflow drought is interpreted as exceptionally low with respect to what is expected in a certain part of the year. The actual quantile chosen for the varying threshold is selected later, based on the quality of the forecasts of derived streamflow drought indices and the robustness of the results.

In addition, the quantile-based threshold was calculated separately for observed and forecast runoff, using either an observation climatology or a climatology assembled of past forecasts. This is a very simple way to correct for systematic additive error (bias) in runoff forecasts. Using the same threshold for observations and forecasts would possibly result in a systematic over- or under-forecasting of streamflow drought events. By choosing separate thresholds for observed and for forecast runoff based on the same frequency of occurrence, we can assure this bias will not affect the
verification results of streamflow drought duration. Possible nonlinearities in the prediction bias could, however, influence the verification results of streamflow drought severity and magnitude. Besides that, the forecast error could vary with lead time. Therefore, a lead time dependency of the streamflow drought threshold was implemented by deriving the threshold from a climatology of forecasts stratified by its lead time. After all, a bias could be removed by, e.g., statistical post-processing. However, well-calibrated forecasts of rare events require a large training dataset, which is why this simple method is preferred.

Within the 32-day forecast range, the events of observed or forecast runoff falling below the streamflow drought threshold were detected and the streamflow drought indices were calculated. In addition to that, the timing of each streamflow drought event was calculated as the center time between onset and end of an event. If more than one event was detected within a forecast interval of 32 days, the longest consecutive period of low streamflow was considered as the forecast/observed event. Forecast and observed events do not necessarily have to overlap, neither between forecast and observation nor between the ensemble forecast members. The forecast system is reduced with the objective to answer the following questions: what is the longest expected streamflow drought event within the next 32 days and was such an event observed? In the case of probabilistic forecasts, the question is different: what is the probability of exceeding a streamflow drought event of \(x\) days duration (\(y\) mm severity; \(y/x\) mm day\(^{-1}\) magnitude) within the next 32 days? By doing so, an imprecise timing of the forecast low streamflow event does result in a less strong degradation of the verification score. For events truncated by the limited forecast range of 32 days, an influence on the verification score caused by deficiencies in forecast timing cannot be excluded. In the here used forecast data, 29% of the events are still prevalent at the end of the forecast range at day 32.

Duration, severity and magnitude of streamflow droughts are clearly not independent as they are all calculated from the same set of events. For example an event of long duration is likely to be very severe as well. Their forecast performances are therefore expected to be similar. Still, the different indices should reflect the demands of different interest groups to a streamflow drought forecast. For hydro-power production, for example, the severity might be of paramount interest, whereas for power-plant cooling the duration is more crucial.

### 2.5 Verification scores

The focus of the verification of ensemble streamflow drought index forecasts is set on the value they have for potential forecast users. A score, designed to give the value of a forecast depending on the vulnerability of a forecast user to a certain event, is the relative value or value score (Murphy, 1977; Richardson, 2000; Roulin, 2007). The user is supposed to take preventive action whenever a forecast is issued with a probability exceeding the user’s personal cost-loss ratio. Loss is the customers expense when being struck by an event without any preparation. Cost is what the user would spend on taking preventive action. The value score then gives the relative economic gain for the user when following the advice of the forecast, compared to having only the climatological event frequency as a basis for decision-making. The value score varies between \(\leq 0\) (no additional forecast value) and 1 (perfect forecast). Note that even if the value score equals 1, the user still has to bear the costs for taking preventive action. The value score is calculated for probabilistic forecasts of exceeding a threshold. It gives a value for each possible probability the prediction system can issue, depending on the cost-loss ratio. The upper envelope of all value curves gives the value of the prediction system.

Another score, designed to give an intuitive measure of the prediction system performance, is the generalized discrimination score, or two alternatives forced choice score (2AFC) (Mason and Weigel, 2009; Weigel and Mason, 2011). The score is based on pairs of observations and forecasts. It reflects the forecast performance in discriminating between different observations. An appealing property of the score is its applicability for ensemble, probabilistic, dichotomous, polychotomous or continuous forecasts and corresponding observations. Here, as an illustration, we give the formula for probabilistic forecast; for all other possible combinations of forecast and observation type, referred to Mason and Weigel (2009) and Weigel and Mason (2011). Let \(n_1\) be the number of observed events \(i\), \(n_0\) the number of nonevents \(j\). With \(p_{1,i}\) respectively \(p_{0,j}\) as forecast probabilities for events that respectively did not occur, the 2AFC score is calculated as

\[
2\text{AFC} = \frac{1}{n_0 n_1} \sum_{i=1}^{n_0} \sum_{j=1}^{n_1} I \left( p_{0,i}, p_{1,j} \right)
\]

applying the rule

\[
I \left( p_{0,i}, p_{1,j} \right) = \begin{cases} 
0.0 & \text{if } p_{1,j} < p_{0,i} \\
0.5 & \text{if } p_{1,j} = p_{0,i} \\
1.0 & \text{if } p_{1,j} > p_{0,i}.
\end{cases}
\]

A 2AFC score above 50% is reached if the forecast is better than a guess based on climatology, hence skillful, assuming that the forecast/observation sample is representative for the climatological regime. A perfect forecast scores 100%. The 2AFC score gives an intuitive measure of the frequency of correct forecasts. Here, the 2AFC score is used to evaluate ensemble predictions against observed runoff, or probabilistic predictions (probabilities to exceed a threshold) against dichotomous (i.e., \(\in \{0, 1\}\) observed outcomes, depending on the context.
3 Results

In this section, the forecast quality for different flow regimes is evaluated on a daily basis as well as for scenarios described by the streamflow drought indices. This comprises the choice of a daily varying streamflow drought detection threshold and the assessment of the quality and impact of the initial conditions. The economic value of streamflow drought index forecasts is given for different interest groups.

3.1 Extended lead-time forecast quality

One basic hypothesis of this study is the better predictability of low streamflow events than peak-flow events. As a consequence, longer range forecasts of streamflow droughts should prove useful for end users. To back up this hypothesis, it is tested how well the forecast system can predict the probability to exceed different thresholds, from very low to very high runoff, depending on the forecast lead time. A number of ascending quantiles from the complete gauged Thur runoff time series available are used as thresholds. The thresholds are, as described in Sect. 2.4, calculated on a daily basis. Some of the lower quantiles can be seen in Fig. 2. Figure 4a shows the 2AFC score for forecast probabilities to exceed these thresholds for lead times from 1 to 32 days. The results support the hypothesis. Peak flow forecasts, i.e., exceedance probabilities for the 80th quantile and above, show very little to no skill past about day 15. In contrast, probabilistic low streamflow forecasts, e.g., for the 20th quantile, are skilful up to the end of the forecast range. At low thresholds, the forecast quality decreases less rapidly with growing lead time. A very similar picture is obtained when using the relative value score. Figure 4b shows the maximum of this score for any cost/loss ratio. Peak-flow forecasts show no relative value past a lead time of 15 days, whereas probabilistic forecasts of low streamflow are valuable over the entire forecast range. Relative values greater than 0.6 are possible up to a lead time of 15 days and more than 0.1 at 32 days. For both plots in Fig. 4, not significantly skilful score values are colored white. This was tested by resampling the underlying verification data 1000 times with replacement and applying a t-test with a confidence level of 0.95 to see whether the score mean was significantly larger than the smallest value considered as skilful.

The long-term predictability of streamflow drought events might be attributed to the persistence of the initial state of the model. Conceptually, the recession rate of streamflow is a function of the streamflow itself (e.g., Kirchner, 2009). The lower the streamflow, the slower any further reduction occurs. Consequently, a good initialization of the prediction model is especially crucial for forecasts of streamflow drought events. If the initialization leads to a surplus of runoff, for example, the streamflow drought threshold might not be crossed within the forecast range or, at least, the forecast timing would be poor.

The dependence of forecast quality (in terms of the 2AFC) on the quality of the initial state for high and low runoff regimes is shown for lead times from 1–32 days in Fig. 5. The plot shows the 90 % confidence limits (from 5 % to 95 %) found by random resampling of the dataset 1000 times with replacements. As no observations for the initial state variables are available, the separation between good and poor initial states is based on runoff. It is assumed that a good initial state, provided by the reference run, results in a predicted runoff close to the observed runoff. Hence, the difference in runoff between both is taken as a measure for the quality of the initial state. In order to get a clear signal, we consider an initial state as good if the predicted runoff at initialization deviates less than 25 % from the observed runoff, and as poor if it deviates more than 75 %. For both groups low- and high-flow regimes are considered separately by verifying the probability of daily runoff to exceed the 85th and the 15th quantile. In the low runoff regime, a good initial state can contribute to forecast skill over the complete forecast range of one month. The effect of a good initialization on the

Fig. 4. 2AFC and maximum relative value scores for the Thur VarEPS/PREVAH daily mean runoff forecasts up to a lead time of 32 days. In the study period 1991–2008, probabilities of the ensemble forecasts to exceed different, quantile-based, varying thresholds are verified.
3.2 Choice of the streamflow drought detection threshold

To proceed from forecasts of daily runoff to forecasts of streamflow drought indices, a threshold needs to be selected. Therefore, the performance of low streamflow index ensemble predictions, according to the choice of thresholds used to define a streamflow drought event, is evaluated next. The result of this analysis should give an indication about which threshold would be most appropriate for the subsequent verification of the streamflow drought index forecasts. Figure 6 shows the verification results of ensemble duration, severity and magnitude forecasts for streamflow drought detection thresholds from the varying 5th to 50th quantile of Thur runoff. The boxes indicate the range and inter-quartile range found by 1000 times random resampling of the dataset. For all indices, the overall forecast performance appears to be better if a lower threshold is chosen. Duration forecasts degrade most strongly with higher thresholds, but stay skillful with a 2AFC score of 67% when using the 50th quantile. Severity forecasts reach a 2AFC score of about 70% for the 50th quantile, and the magnitude forecast skill stays constant at about 72% within the uncertainty bounds when varying the threshold. The decrease in forecast skill with increasing threshold can be attributed to the enlarged uncertainty in the forecast itself. The higher uncertainty about the score at lower thresholds is a result of the lower number of events. For the subsequent evaluation of streamflow drought index forecasts, a threshold based on the varying 15th quantile is applied, resulting in 529 events detected for 954 ensemble forecasts (Fig. 6). The choice of the 15th quantile is a compromise between the number of streamflow drought events and the significance of the findings regarding low streamflow. The runoff associated with the 15th quantile, i.e., the streamflow drought detection threshold used for our research catchment, can be deduced from Fig. 2. A distinct seasonal runoff maximum occurs in April due to the contribution of snowmelt. The yearly minimum is reached in October or November, when snow accumulation starts.

3.3 Streamflow drought indices prediction/observation

As already shown, the quality of a streamflow drought forecast relies greatly on the quality of the representation of the catchment initial state in the hydrological model. This initial state is taken from a reference run, forced with meteorological surface observation. Usually, without having measurements of the state variables of hydrological models available, one way to infer the quality of the initial state is to look at a good reproduction of runoff by the reference run. Figure 7 shows the occurrence (therefore indirectly the duration), severity and magnitude of streamflow drought events at the runoff gauge in Andelfingen during the study period 1991 to 2009, as observed or predicted by the reference run. As a streamflow drought detection threshold of varying quantiles is used, the events are distributed evenly over the year. The most severe events and the events of greater magnitude however mostly occur in late spring/early summer, when the runoff reaches the yearly maximum due to the contribution of melting snow. The high quality of the reference run already mentioned is also reflected in its representation of the streamflow drought indices. A high degree of agreement between observation and reference can be seen in the occurrence and timing of the events. High severities and magnitudes in the observations are also strong events in the reference run, although the absolute number can vary. Altogether, the initial states seem to provide a reasonable basis for the initialization of forecasts.

Ensemble forecasts of streamflow drought duration, severity and magnitude, utilizing a threshold based on the varying 15th quantile of runoff, are shown in Fig. 8 together with the corresponding observations. The plot shows the range of the weekly started forecast streamflow drought indices, valid for the next month. To enhance readability the observed indices and the forecast ranges are concatenated. Duration and severity of the observed streamflow drought are contained well within the range of the ensemble, although it appears that the forecasts have a tendency to overpredict the events. The characteristics of duration, severity and magnitude forecasts are very similar to each other as they are derived from the same streamflow drought events. Note that, due to the weekly start of the forecast, each day is covered by three forecasts. A very long event is therefore captured by several forecasts. For some
forecasts such an event can exceed the forecast range, or a forecast might start during an event. As in observation and reference run, the occurrence of streamflow drought events is distributed equally over the year in the forecasts, which was expected as the detection threshold varies with season. One noticeable feature that can be seen in the ensemble forecasts and the observations is the distinct signal left by the 2003 drought caused by a heat wave that affected large parts of Europe (Beniston, 2004; Schär et al., 2004; Zappa and Kan, 2007).

The first impression of over-forecasting is confirmed by the rank histograms (Talagrand et al., 1997) in Fig. 9. A disproportionately large part of observations fall in the lower bins spanned by the ensemble members. This lack of reliability is most distinct for magnitude forecasts, and less for forecasts of duration and severity. However, the discrepancy between the forecast probability and the observed frequency is a type of error that could possibly be corrected for with a statistical post-processing. Such a model bias was partly corrected for by using separate detection thresholds for observations and for forecasts.

3.4 Relative economic value

The economic value of probabilistic forecasts of streamflow droughts, exceeding different levels of duration, severity and magnitude was calculated for forecast probabilities using the 15th quantile streamflow drought detection threshold (Fig. 10). Value scores > 0 are shown for a variety of forecast users, characterized by their individual cost-loss ratio. It appears that, for all thresholds and indices, valuable forecasts for certain user groups can be produced. Especially risk-averse forecast users with low cost-loss ratios would benefit from ensemble forecasts for events of long duration or high magnitude and severity. In contrast, forecasts of longer, more severe events have no additional value for users with higher cost-loss ratios. These users would benefit from probabilistic forecasts of less intense events. For all users with cost-loss ratios < 0.6, i.e., especially the risk-averse users, value scores > 50% are possible. The same evaluation was performed for streamflow drought index forecasts using a higher or lower streamflow drought detection threshold (not shown). In accordance with Fig. 6, higher value scores are possible with the 5th quantile, and lower scores with the 50th quantile as detection threshold. The highest value score for each threshold is reached where the cost-loss ratio concurs with the climatological frequency of the event. This property of the value score is the reason for the shift to the left with increasing thresholds. The maximum of the value score, however, is not strongly dependent on the duration, severity or magnitude of the event and is here reaching values of 0.4–0.6.

A direct comparison of the forecast quality of streamflow drought indices with the quality of probabilistic daily predictions as shown in Fig. 4 is not possible, as streamflow drought events typically cover several days and no longer contain information about the lead time. The loss of predictive skill of daily probabilistic forecasts with growing lead time has already been addressed (Fig. 4). In comparison, the maximum value score of probabilistic streamflow drought index forecasts is not strongly dependent on the duration, severity or magnitude of the event. As the timing of the streamflow drought events is not exactly specified, but is somewhere between day 1 and day 32, the value score for the events ranges around the lead time averaged value score of the probabilistic daily forecasts as shown in Fig. 4b.

3.5 Timing

One drawback when forecasting streamflow drought indices instead of the full hydrograph is the lack of information obtained about the timing of the event. An approach to evaluate this forecast characteristic is to consider timing as the center time between event onset and end of the event or forecast, as described in Sect. 2.3 or Fig. 3. The median of the ensemble of forecast timings is evaluated against the observed timing. Due to the forecast range, the timing is restricted to 32 days, whereas this limit can only by reached by events starting on the last day of the forecast. A concentration of events will have a timing around 16 days, because the longer the event, the closer the timing has to be to the center of the forecast range.

The performance of the forecast system in predicting the timing of events is assessed by having a closer look at the
Fig. 7. Periods of streamflow drought occurrence, with severity (A and C) and magnitude (B and D) indicated by colors. (A) and (B) are derived from the observed runoff, while (C) and (D) are derived from the reference run.

Fig. 8. Concatenation of weekly issued ensemble forecasts of streamflow drought duration, severity and magnitude from the 32-day lead time VarEPS-driven reforecasts (ensemble range shaded in gray), and corresponding observations (black line). The threshold to characterize a streamflow drought event is the varying 15th quantile of runoff. Although the forecasts and observations are not continuous, the data are presented as lines to enhance readability.
cases when a forecast streamflow drought event was observed. Of all forecast events, 46 % had a counterpart in the observations (hit rate), and 32 % were missed or false alarms. Figure 11 shows how the timing of the observed event relates to the ensemble median of the predicted timing for the 42 % of hits. The data exhibit a lot of scatter, but, as underlined by the 2-d density map, the forecast timing can explain 22 % of the variance in the observed timing. In order to attribute a forecast event to an observed event, the events should at least for one day overlap. This is the case for 49 % of all hits.

4 Discussion and conclusions

Eighteen years of weekly initialized, hydrological ensemble forecasts of daily mean runoff for the Thur catchment in Switzerland, with a lead time of 32 days, were evaluated. The focus was on their potential to provide skillful, and thus valuable, information about the characteristics of streamflow droughts. The basic assumption of a higher predictability of low flow than peak flow was confirmed by the verification results. This was attributed to the fact that long-lived processes dominate the recession behavior of the runoff. For higher flow, in contrast, the quality of the runoff forecasts is strongly dependent on the correct timing and the amount of precipitation given by the meteorological forcing model, limiting predictability. The positive effect of good initial states on the forecast quality is quickly lost in those cases. This was also confirmed for catchments prone to flash floods, where the influence of initial conditions was found to be already lost after just a few hours (Zappa et al., 2011).

It was further found that, for the predictability of streamflow droughts, a good representation of the hydrological model states at forecast initialization is essential. In a low runoff regime, a good initialization can be beneficial for the forecast for a much longer range. A possible explanation would be that the initial state variables contribute on different time scales to the produced runoff. They therefore determine the recession behavior, which is crucial for the forecast of streamflow drought events. Consequently, good initial states can contribute to forecast quality in a low runoff regime over a longer range. Shukla and Lettenmaier (2011) as well as Singla et al. (2012) similarly stress the importance of the initial conditions for lead times of up to one month, depending on the climatic conditions. In this study, a comparison of the observed runoff with the runoff from a reference run indicated the good quality of the used initial states, legitimating the launch of a subsequent forecast.
Having ensemble forecasts of the streamflow drought indices duration, severity and magnitude at hand was shown to provide additional value to end users. Using those forecasts results in an economic advantage, mostly independent of the duration, severity or magnitude of the event. Compared to daily forecasts, streamflow drought index forecasts are of reduced complexity, as they no longer contain information about the timing of the streamflow drought event. Hence, the forecast system is less penalized when the onset and offset of streamflow drought events are lagged compared to observations, which enhances the value of the forecasts. It was shown that streamflow drought index forecast can reach economical values greater 50% for the more risk-averse users. A comparison of the forecast timing of drought events with the observed timing showed that this information gives only a rough estimate. The forecasts of streamflow drought indices can provide useful information about the characteristics of an upcoming event. The timing prediction should, however, be handled with caution.

The ensemble forecasts evaluated in this study were performed for a relatively large alpine catchment. This was chosen mainly in order to ensure the occurrence of longer periods of low streamflow, as in larger catchments runoff is not as strongly affected by small or local precipitation events. However, we also tested streamflow drought predictions for smaller alpine catchments. There, only shorter streamflow drought events could be evaluated and the value of these forecasts was found to be lower. Nevertheless, streamflow drought index forecasts can still be useful for smaller catchments.

When analyzing streamflow droughts on time scales of one month or longer, it is common to apply a smoothing of the observed or forecast streamflow time series. This should prevent counting shorter streamflow depletions as individual drought events, although they belong to the same larger-scale drought. Such a smoothing is not applied in this study as also short-term water shortages of one day can have an economical impact, independent on whether the single events are induced by a larger-scale drought event or not. Sectors prone to short-term streamflow droughts are, e.g., shipping, hydro-power production or power production in general as the cooling of many power plants depends on the availability of river water. Forecast users from those sectors could potentially benefit from forecast of short events, and this study investigates the potential of a hydrometeorological forecast system to predict them.

Further refinements could improve the predictability of streamflow droughts. The parameters of the hydrological model PREVAH were found by optimizing the predicted runoff subject to average flow volume. This is certainly not the best approach for streamflow drought forecasts and might introduce biases in predictions of the lower flow regime. Our findings, however, suggest that an operationally used hydrological prediction system, which is meant to give warnings primarily of peak flow, can without larger modifications also be suitable for forecasting streamflow droughts. Biases due to inadequate model parameterization can be partly addressed by a simple statistical post-processing, e.g., defining the streamflow drought threshold for the observed runoff from an observation climatology and for forecast runoff from past model predictions. More complex methods could be considered, but this was beyond the scope of this study.

The downscaling of the meteorological model could be further improved. In this study, the relatively coarse horizontal grid of the meteorological forcing model was downscaled to the grid of the hydrological model by a simple bilinear interpolation. A dynamic downscaling involving one or more nested regional models would be preferable. However, no such approach was available for the region and the forecast range of one month considered here.

The operational version of the meteorological forcing model VarEPS would offer 51 ensemble members compared to only 5 members from the reforecast. As a low number of ensemble members introduce low reliability in the forecast (Weigel et al., 2007), the here shown verification scores reflect the lower limit of what can be achieved with the full ensemble. Despite the limitations, ensemble forecasts of streamflow drought indices could provide a valuable basis for decision-making and be of economic value for forecast users.
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