Geophysical methods to support correct water sampling locations for salt dilution gauging

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Abstract. To improve water management design, particularly in irrigation areas, it is important to evaluate the baseline state of the water resources, including canal discharge. Salt dilution gauging is a traditional and well-documented technique in this respect. The complete mixing of salt used for dilution gauging is required; this condition is difficult to test or verify and, if not fulfilled, is the largest source of uncertainty in the discharge calculation. In this paper, a geophysical technique (FERT, fast electrical resistivity tomography) is proposed for imaging the distribution of the salt plume used for dilution gauging at every point along a sampling cross section. With this imaging, complete mixing can be verified. If the mixing is not complete, the image created by FERT can also provide a possible guidance for selecting water-sampling locations in the sampling cross section. A water multi-sampling system prototype aimed to potentially take into account concentration variability is also proposed and tested.

The results reported in the paper show that FERT provides a three-dimensional image of the dissolved salt plume and that this can potentially help in the selection of water sampling points.

1 Introduction

Improved management of water resources is becoming more important as several areas of the world suffer from water shortages. Therefore, correct evaluation and preservation of water resources is essential. An important starting point for improving management design is to evaluate the baseline state of the resources, including the amount of discharge from watercourses and irrigation canals.

The most common approach for measuring discharge is the velocity–area method, which involves measuring water depth and velocity at points across a stream section with a current meter. An alternative method of stream gauging involves the injection of a chemical tracer and the evaluation of its dilution following its complete mixing into the stream (Rantz, 1982). This last method is often referred to as dilution gauging: for example the measure of electrical conductivity (EC) as a function of time in a measuring section is performed and related to ion concentration; this last measurement is integrated over time to obtain the discharge value.

Dilution gauging is frequently used in open channels to investigate superficial flows, especially in mountainous streams where the irregular, boulder-laden cross sections and the strong turbulence decrease the accuracy with which depth and velocity can be measured (Moore, 2004; Radulovic et al., 2008). Different types of tracers have been used for dilution gauging; NaCl (in ionic form) is the most frequently used one (Drost, 1989; Zellweger, 1994; Kumar and Nachiappan, 2000; Tazioli, 2011).

Dilution gauging is commonly performed by either a constant flow injection or an instantaneous slug injection. The constant injection allows for high accuracy, and it is used especially, and almost exclusively, for low flows (discharges less than approximately 0.1 m³ s⁻¹; Moore, 2005). On the other hand, the instantaneous slug injection can be used for higher discharges (flows up to 10 m³ s⁻¹ or greater; Moore, 2005) and in more logistically complicated areas because the
measuring equipment is very easy to move. The only disadvantage of this last methodology is the amount of NaCl that needs to be added that is primarily linked to the background EC level; different discussions can be found in the literature in this respect (Gees, 1990; Kite, 1993; Hudson and Fraser, 2002; Moore, 2005).

An important issue of dilution gauging is that the method requires a complete vertical and lateral mixing of the tracer at the sampling site, without tracer losses or gains between the injection site and the measurement site. Vertical mixing typically occurs more rapidly than lateral mixing (Rantz, 1982). The dynamics of mixing will vary based on the hydraulic characteristics of the given reach. Frequently, long reaches are needed to ensure a complete lateral mixing of the tracer. An optimum mixing length is generally the one that allows for adequate mixing but does not require an excessively long sampling duration. When the slug injection method is used, complete mixing is considered to have occurred when the concentration is uniform at every point of the cross section at the sampling location. If the adequate mixing is not certain at a given sampling location, the tracer must be sampled for its entire transit time at several locations throughout the sampling cross section of the channel. Rantz (1982) has found that at least three lateral sampling points should be used regardless of stream characteristics. Several empirical equations that take into account the different canal features (gross estimated discharge, width, etc.) and the type of tracer injected can be found in the literature to determine the mixing length (e.g., Moore, 2005; Jaramillo, 2007). These equations commonly provide inaccurate estimates as they often underestimate the mixing length. Apart from these specifications, no particular precautions are proposed in the literature for directly verifying the complete lateral and vertical mixing of the tracer.

Indirect geophysical measurements, such as electrical resistivity tomography (ERT), can potentially be applied to evaluate mixing. ERT usage has been developed in recent decades as a monitoring tool (Xie et al., 1995; Tapp and Wilson, 1997) and can be profitably used to image component concentration distributions and detect dynamic changes in a multi-phase processes. Moreover, quantitative evaluations about the properties of the imaged water can be accomplished using one of the various relationships relating the electrical resistivity to the physical and chemical properties of the water mixture. Most of the applications presented in the literature (Fangary et al., 1998; Lucas et al., 1999; Wang and Cilliers, 1999; Yang and Liu, 2000; Warsito and Fan, 2001) address cylindrical flows (in pipes, cyclones, tanks), and the electrodes are placed on one or more circumferences orthogonal to the cylinder axis. This geometrical configuration assures an optimum conditioning of the inverse tomographic problem, but its applicability to real case studies on natural rivers or channels is limited. A number of previous studies have focused on situations where the imaged body cannot be entirely surrounded by electrodes, as in the case of creeks, rivers and canals. This has been performed in slow water flows (Sambuelli et al., 2002) to assess the possibility of recognizing the presence of granular materials and in fast water flows in the laboratory (Sambuelli and Comina, 2010) to image solid and pollutants flowing through a canal cross section. In this last application the fast electrical resistivity tomography (FERT), proposed in this work, has been already tested under controlled conditions. FERT has the advantage of allowing for very fast monitoring of the flow due to the high speed of acquisition of the tomographic images. This capability extends the field of applicability of common ERT methods.

The objective of this study is to evaluate the potential of FERT to image the cross-sectional distribution of an NaCl (in ionic form) plume, used for dilution gauging, in a real case study. Because the knowledge of tracer distribution throughout the measuring cross section is crucial to correctly position the sampling points, FERT can be potentially used as a preliminary control. Providing an image of the plume would help in selecting appropriate sampling points and establishing a more accurate section for dilution gauging. FERT images are also compared with direct local measures of the same NaCl (in ionic form) plume. These are performed by means of a water multi-sampling system prototype developed for simultaneous sampling at different points along the cross section. A comparison of the results is discussed with the aim of evaluating the potential of FERT as a guide for the correct location of water sampling points.

2 Methods

After a brief introduction to the test site, the conceptual basis and field procedures for slug injection using dilution gauging and geophysical controls are hereafter presented. In particular, the water multi-sampling system prototype, proposed for the optimization of tracer detection, is described together with the field procedures necessary for the execution of FERT.

2.1 The study area: the Osasco Canal

The Osasco Canal is an irrigation canal located in Piedmont (northwest Italy). It has an overall length of 7 km and carries water diverted from the Chisone River (Fig. 1). The canal reach where our tests were performed has a mean width of 2 m and a water depth of approximately 0.5 m. The Osasco Canal has an average gross discharge of 0.5 m$^3$ s$^{-1}$, estimated with the velocity–area method, quite variable over time, and a constant water EC of 170 µS cm$^{-1}$ (Clemente et al., 2013; Perotti et al., 2013). The EC monitored in the canal shows little variation throughout the day. Given the variability of the dimensions of the rectangular canal section and estimated average flow velocity, the flow regime of the canal is considered turbulent but placid (Scobey, 1939). The mixing
length estimated from empirical relationships (Moore, 2005; Jaramillo, 2007) is approximately 50 m. To ensure an adequate testing length, a canal reach of 100 m was chosen (Fig. 1).

Pictures of both the sampling and the injection points are shown in Fig. 2. In the studied reach the bottom of the channel is cobbled (gravel and cobbles), except for a small portion immediately upstream of the chosen injection point, where a small cemented weir is located (Fig. 2). The measuring section is located under a small road bridge, and a canal curve is located immediately downstream of this section (Fig. 2).

The most appropriate reach was chosen considering the following: (1) the reach has no dead water between the injection and sampling points; (2) the sampling site is free of air bubbles caused by excessive turbulence that interfere with EC measurements; (3) the injection point appears to be turbulent enough to ensure the tracer mixing; (4) the background EC level of the river is stable during the measuring time; (5) the reach length is consistent with the estimated mixing length.

2.2 Slug injection method

In this study NaCl (in ionic form) was used as a tracer: a mass of 9 kg was dissolved in a barrel in approximately 30 L of water and was instantaneously injected into the canal at the injection point (Fig. 2). Fluorescein was also added to the salt–water mixture to have a qualitative visualization of its passage in the measuring section. The basic principle is that the ionic NaCl concentration in the slug increases the natural water concentration; this increases the measured electrical conductivity (EC), which can be used as an index of the salt concentration. Over a wide range of concentrations, the EC is indeed linearly related to salt concentration (Radulovic et al., 2008; Moore, 2005; Gees, 1990; Rantz, 1982) so that the EC response can be transformed in ionic concentration of NaCl.

The equation for computing stream discharge, which is based on the principle of the conservation of mass, is (Rantz, 1982)

$$Q = \frac{V_0 \cdot C_0}{\int_0^\infty (C_t - C_b) \, dt},$$

(1)

where $Q$ [m$^3$ s$^{-1}$] is the discharge of the canal, $V_0$ [m$^3$] is the volume of the tracer solution injected into the canal, $C_0$ [mg L$^{-1}$] is the concentration of the solution, $C_t$ [mg L$^{-1}$] is the measured tracer concentration at a given time $t$ at the downstream
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The term \( \int_0^\infty (C_t - C_b) \, dt \) represents the total area under the concentration–time curve. To obtain this curve the passage of the entire tracer plume was monitored by measuring the EC of the water at the sampling section at a sampling interval of 5 s. Measurements were continuously recorded for approximately 5 min during the passage of the salt plume. The values of the EC curve were then transformed into concentrations through the use of a laboratory-estimated calibration curve. This calibration was constructed by measuring the variation of EC in a sample of the canal water to the addition of different amounts of NaCl. The concentration with respect to the natural water conductivity, which is used as reference, is therefore obtained. A highly coherent calibration curve with an \( R^2 \) squared value almost near unity has been obtained:

\[
C = 5.3 \times 10^{-4} \cdot \sigma - 9.6 \times 10^{-2},
\]

where \( C \) is incremental ionic concentration of NaCl [g L\(^{-1}\)] and \( \sigma \) is conductivity [\( \mu \text{S cm}^{-1} \)].

2.3 Sampling optimization

To obtain an EC value that is more representative of the entire sampling cross section, a water multi-sampling system prototype was devised. This system was created with a framework of steel rods to which nine tubes with a small diameter are connected. The tubes are attached to a single water pump which spills the water simultaneously from the nine measuring points – mixing all nine samples and producing an average value at each sample interval. This apparatus allows for a more extended sampling of the whole canal section and reduces, through averaging, the uncertainty due to an incomplete tracer mixing. However, the geometry of the measured section (different water depths along it) and the limited manoeuvrability of the whole system allowed for the sampling of only a portion of the canal section. A scheme of the adopted multi-sampling system and of its location is reported in Fig. 3.

2.4 Cross-flow FERT

Cross-flow FERT has been implemented by means of an array of 16 underwater electrodes (14 on the canal bottom and 2 on the sides). The electric cable has been anchored on the canal bottom by means of appropriate weights, and the position of each electrode together with the shape of the section has been measured. The electrode positioning scheme for the test site and a picture of the array is shown in Fig. 4.

The electric cable has been connected to an A.C. georesistivimeter (CIT Iridium Italy s.a.s.) injecting a sinusoidal current at 916 Hz. The CIT is a very fast acquisition device with 16 bit resolution. The instrument, at the selected frequency, can execute approximately 20 acquisitions per second. An acquisition sequence consisting of a total of 227 quadrupoles (both dipole–dipole and Wenner types) has been used. For the experimental setup of this study, the time required for the acquisition of a single tomography data set was on the order of 30 s (of which 11 s of real acquisition time) including saving the file and starting up the new measurement. Measurements were continuously collected for approximately 5 min during the passage of the salt plume, and several tomographic data sets were obtained. To obtain the resistivity images from...
the collected data, we used a software (NES Electric Arbitrary 2-D Closed Geometry by Andrea Borsic) based on a damped least-squares inversion algorithm.

A time-lapse analysis calculating the relative difference in electric resistivity (ER) of the acquired images during the plume transit with respect to a reference image was then performed. The reference image was achieved from the mean of three FERT measurements carried out before the slug injection (ER of 58 Ωm coherently corresponding to the inverse of the EC of 170 µS cm⁻¹ directly measured in the canal). With this representation, the passage of the salt plume is expected to show an overall reduction in resistivity (increased concentration of the salt plume) throughout the images. The same laboratory calibration curve used for dilution gauging was subsequently used to convert the resistivity images in salt concentration images.

3 Results

The measured breakthrough curve from the direct sampling with the adopted multi-sampling system is reported in Fig. 5; for convenience of comparison with the results of cross-flow FERT, the data have been converted in ER. The discharge, evaluated with Eq. (1), resulted in 0.46 m³ s⁻¹. The main peak evidenced from this curve was approximately 14 Ωm corresponding to an EC of approximately 700 µS cm⁻¹ and to a peak concentration of 0.27 g L⁻¹. In Fig. 5, the times when the FERT images were acquired are also reported.

The results of some FERT images during the passage of the salt plume are presented in Fig. 6; some of the images, with very similar ER distributions, have been suppressed (dashed lines in Fig. 5) to simplify visualization. In these images the ER differences with respect to the condition without artificial tracer are reported. The images show clear evidence of the passage of the salt plume, correctly identified with a strong resistivity reduction. This reduction is quite homogeneous at early times, corresponding to the higher salt concentration in the plume, but appears more concentrated in some zones of the canal in the tail of the plume. The left side of the reconstructed resistivity image (which is upstream of the canal curve) appears not to be affected by the passage of the plume. This has also been observed on site by visual inspection of the passing colored plume. The reduction in resistivity has an average value of approximately −25 Ωm with respect to the clear water, even if localized, more marked reductions (approximately −30–35 Ωm) are present in the map.

As expected, mainly due to the different sampling time (see also discussion below), the average reduction is a little lower than what was obtained from the direct sampled curve which instead reports a peak reduction of approximately −40 Ωm with respect to the canal resistivity without artificial tracer (from 58 Ωm to approximately 14 Ωm; Fig. 5).

The resistivity images acquired have been then transformed to extract quantitative information about the salt concentration. Such data are reported in Fig. 7, for the same sampling intervals of Fig. 6, and in Fig. 8 in a 3-D representation. The leading edge of the salt plume is clearly evidenced in both images and appears relatively uniform. This suggests that mixing is fairly uniform in early stages. However, at later time intervals, some localized peaks in concentration appear. Particularly in the 3-D interpolation the tailing edges of the plume reveal high concentration zones along the banks of the canal. Because dead zones do not seem to be present in the measuring reach, the results confirm the supposed turbulent but placid flow regime. Indeed the velocity of flow varies from zero at the walls to a maximum in the center, as evidenced by preliminary qualitative tests using a current meter. This is reflected in the two main concentration peaks located on both sides of the measuring section, and only one of them appears to be correctly sampled by the direct method since the sampling grid has been placed closer to the left downstream bank (Fig. 3).

By extracting mean and standard deviation values of the concentrations in every tomographic image, it is possible to obtain a trial estimate of the time–concentration curve from geophysical measurements. This interpretation is reported in Fig. 9 and compared to the one obtained from direct measurements. As expected, the mass balance of the injected salt extracted from the two evaluations (i.e., multi-sampling system and cross-flow FERT) differs slightly. The mean values of cross-flow FERT data report a lower concentration peak (approximately 0.1 g L⁻¹) with respect to the directly sampled curve.

4 Discussion

FERT images have to be used primarily as a qualitative tool for evaluating the homogeneity of the plume. There are indeed several reasons that must be taken into account to explain the observed differences between multi-sampling system and cross-flow FERT results. These are mainly related to the limitations in quantitative FERT analysis but also in the different location of imaging and sampling points. These observations can be resumed hereafter:
1. The concentration extracted from cross-flow FERT is an integral concentration over the measuring time, and it takes 30 s (of which 11 s of real acquisition time) to acquire the data used in each image. It is therefore possible that part of the plume passing in the measuring section is lost during acquisition. Moreover the measuring sequence requires the shifting of the different quadrupoles to different positions along the section during this time interval which is higher than the one used for direct sampling (5 s). Therefore FERT image interpretation will most likely produce a reduced concentration peak value given the speed of the phenomenon under observation.

2. The reduced peak concentration observed by cross-flow FERT may also be related to the smoothing of the inversion algorithm adopted, which does not allow for variations that are too sharp in conductivity and therefore in concentration. When the concentration distribution within the section is irregular because of spotty and high concentration values, the inverse solution has increased variability. Notably, the larger standard deviation error bars, which, regardless of the statistical distribution of the data, are an index of dispersion around an average value, are larger near the peak of the plume and smaller towards the end of it.

3. Cross-flow FERT images the whole section of the canal including the left bank zone where there appears to be a reduced concentration area; therefore, with respect to the direct sampling technique, it has the potential to evaluate the entire plume distribution. This results in a more reliable visualization of the plume, and the reduced concentration peak observed could also be partially related to the lower concentration zone near the left bank.

4. The multi-sampling system can be affected by localized high concentration points, which could partially bias towards higher concentrations in the overall estimate. Indeed if the maximum concentration value is considered from cross-flow FERT data, the two curves seems to be in better agreement (dashed red line in Fig. 9).

Notwithstanding the mentioned limitations of the FERT method, a quantitative estimation of discharge has been attempted, over the imaged section, and compared with the discharge given by the multi-sampling system. Equation (1)
Figure 7. Concentrations in the imaged section for increasing times (over about 30 s intervals), image number and time indication with reference to Fig. 5, seen from upstream.

Figure 8. 3-D visualization of the passage of the salt plume in the studied canal section, time axis coherent with Fig. 5.

Figure 9. Comparison of direct sampling and cross-flow FERT obtained concentration curves; the dashed red line refers to the maximum concentration value determined from cross-flow FERT in the area of the canal reported in Fig. 10.

has been applied, as a function of the cumulative concentration for the entire monitored interval, to each point in the imaged section and a representation of discharge variability has been obtained (Fig. 10). Discharge values obtained with the above-mentioned process, depicted in Fig. 10, represent the value that a localized sampling point would acquire if located piecewise within the section. The average discharge evaluated with FERT is globally higher (mean value of 0.72 m$^3$ s$^{-1}$) than the one estimated with the direct sampling method (0.46 m$^3$ s$^{-1}$). In Fig. 10 it can be noted that discharge values are not uniform along the section, and
it can be also observed that some of the spilling tubes appear to be located near low discharge zones (i.e., high concentration peaks) particularly at the bottom of the canal. In these zones the two estimates appear to be more coherent: locally, areas with 0.5 m$^3$ s$^{-1}$ of discharge are evidenced from FERT roughly matching the 0.46 m$^3$ s$^{-1}$ value from direct sampling. The average discharge from direct sampling could be therefore partially biased towards lower values due to the location of the sampling points. The average discharge evaluated from FERT using only values located in the same position of the spilling tubes resulted indeed in 0.59 m$^3$ s$^{-1}$, partially confirming this hypothesis. It must be also observed that anomalous high discharge values at the bottom of the canal are locally present together with zones on the top of the image in which the too low concentrations observed drive the discharge to unrealistically high values. Even if, due to the flow regime, higher discharge is expected particularly near the free water surface (values around 0.8 m$^3$ s$^{-1}$ from FERT), these can be also partially attributed to inverse problem uncertainty and low resolution which, due to the electrodes disposition, is particularly high in the top part of the section. The quantitative evaluations attempted confirmed that, at present, the FERT technique is a powerful imaging tool but still not completely reliable in estimating an accurate discharge value. Only with the development of the technique a space variable quantification of discharge over the testing section could be potentially obtained.

5 Conclusions

Direct sampling of the NaCl (in ionic form) plume from a slug-injection salt dilution test and geophysical imaging of the same salt plume, using cross-flow fast electric resistivity tomography (FERT), have been compared in this work in a single case study. Direct sampling has been performed with a prototype multi-sampling system, obtaining an average value over the sampled area; geophysical data have been acquired and interpreted independently.

The results show that the reconstructed curve from cross-flow FERT seems affected by an overall lower sensitivity with respect to the peak passage of the plume, and therefore mass balance estimates based on these data cannot be considered completely reliable. At present, the FERT technique still suffers from limitations mainly related to the velocity of acquisition and can therefore only offer qualitative representations of the salt plume. Nevertheless, cross-flow FERT has provided a reliable visualization of the passage of the plume in the imaged section, showing some localized low-conductivity zones. Because the knowledge of tracer distribution in the measuring cross section is very important for the correct placement of sampling points, FERT can be potentially used as a preliminary control in this respect. Providing images similar to the ones presented in this study prior to the design of the sampling grid could be very helpful in establishing the most correct direct measurement protocol.

Indeed, discharge measurements by means of the salt dilution method are the most frequently used approaches, especially in difficult-to-access areas: in these situations, testing requirements are often not easily accomplished due to logistical conditions. It is also not always easy to establish a priori whether all the test requirements are satisfied.

Geophysical imaging can therefore be an important aid offering a direct visualization of the salt plume and consequently a more precise location of sampling points. Following this first visualization, a sampling optimization in the downstream sampling section, using a multi-sampling technique, is strongly recommended. Sampling the canal water in different points of a cross section, by means of simultaneous water picking up, can optimize the quantitative detection and results in more reliable discharge estimates.

We are conscious that the single case study presented has to be considered only as a starting point both for the FERT technique and for the multi-sampling prototype apparatus. Further tests in different conditions and flow regimes are planned to result in a more consistent discussion on the topic. Nevertheless the presented case offers a clear description of the potential of the presented methodology to be viewed as a starting point also for other researchers.
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