Effects of snow ratio on annual runoff within the Budyko framework

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Abstract. A warmer climate may lead to less precipitation falling as snow in cold seasons. Such a switch in the state of precipitation not only alters temporal distribution of intra-annual runoff but also tends to yield less total annual runoff. Long-term water balance for 282 catchments across China is investigated, showing that a decreasing snow ratio reduces annual runoff for a given total precipitation. Within the Budyko framework, we develop an equation to quantify the relationship between snow ratio and annual runoff from a water-energy balance viewpoint. Based on the proposed equation, attribution of runoff change during the past several decades and possible runoff change induced by projected snow ratio change using climate experiment outputs archived in the Coupled Model Intercomparison Project Phase 5 (CMIP5) are analyzed. Results indicate that annual runoff in northwestern mountainous and northern high-latitude areas are sensitive to snow ratio change. The proposed model is applicable to other catchments easily and quantitatively for analyzing the effects of possible change in snow ratio on available water resources and evaluating the vulnerability of catchments to climate change.

1 Introduction

More than one-sixth of the world's population lives in catchments with snowmelt-dominated runoff (Barnett et al., 2005), and thus change in snowfall may exert a great influence over available water resources in these regions. In a warmer climate, the rising temperature may decrease the precipitation falling as snow in cold seasons. A decrease in snowfall amount and an increase in temperature can lead to an earlier spring peak river runoff and a reduction in summer–autumn runoff for a given total annual precipitation (Stewart et al., 2005; Godsey et al., 2014). Therefore, the change in the state of precipitation (rainfall or snow) induced by global warming would alter the temporal distribution of intra-annual runoff, thereby increasing the possibility of spring flood disasters (Allamano et al., 2009) and summer water supply crises in relevant regions. Although the possible events can have catastrophic impacts on those snow-dominated basins, these impacts can be mitigated where existing reservoirs possess adequate storage capacity to buffer the shift in runoff timing (Vörösmarty et al., 1997; Payne et al., 2004). To date, however, little work has been done to investigate the impact and mechanism of this shift in the state of precipitation on mean annual runoff which is a key factor that controls the available freshwater resources for domestic and agricultural needs. Berghuijs et al. (2014) conducted a preliminary analysis using the Model Parameter Estimation Experiment (MOPEX) data set and found that a higher snowfall fraction is statistically associated with increased annual runoff at pristine catchments. They also pointed out that mechanistic understanding of this phenomenon is still lacking. Inspired by Berghuijs et al. (2014), we aim to understand and quantify the relationship between the snow ratio of precipitation falling as snow to total precipitation and mean annual runoff, as well as assess the hydrologic response to snow ratio variation induced by climate change in this study.

In order to address the problem, adopting a distributed hydrological model coupled with global circulation model (GCM) projections and calibrated with observed data may be a way (Cayan et al., 2008; Huss et al., 2008). However, large numbers of parameters and the site-specific nature of distributed models limit us to clarify the dominant factors affecting the connection between snow ratio and mean annual runoff. Furthermore, the distributed model may perform well over short timescales, but large knowledge gaps still remain...
at multi-annual timescale that impede the pursuit of better understanding the effect of snow ratio on mean annual runoff. Meanwhile, it can be a very tedious exercise when quantifying the impact of snow ratio change on the mean annual runoff by applying a detailed hydrologic model to hundreds of catchments.

Low-dimensional models may provide us with an alternative tool to isolate the key component of the relationship between the above two variables. Budyko (1974) introduced a simplified analytical framework to quantify the long-term average hydrologic partitioning between runoff and evapotranspiration at catchment scale. Within this framework, the actual evapotranspiration \( E \) is determined, to the first order, by available energy and available water which are measured as potential evapotranspiration \( E_p \) and precipitation \( P \), respectively. Subsequently, much effort (Fu, 1981; Choudhury, 1999; Yang et al., 2008) has focused on theoretical and empirical development of the framework by introducing an additional parameter accounting for local landscape characteristics (Yang et al., 2009) or seasonality of climate forcing (Feng et al., 2012). This simple framework captures the main features of the water–energy balance and is widely employed to evaluate the hydrologic response to climate change and human activities (Roderick and Farquhar, 2011; Wang and Hejazi, 2011). When addressing the influence of snow ratio on the mean annual runoff, the water–energy balance is also the key point which needs to be clarified. Thus, it is a possible way to investigate the influence of snow ratio on mean annual runoff in the context of the Budyko framework.

Here, we study the effects of snow on the mean annual runoff by analyzing the long-term observed records from catchments across China. A theoretical tool is proposed to help us have a deeper understanding of the role of snow on the mean annual runoff quantitatively. In addition, the contributions of changes in the snow ratio to the variations in annual runoff during the past several decades and possible changes in annual runoff under projected climate scenario are also presented. Such studies are expected to present important implications for future water management strategy when global warming is considered.

2 Data sources

The daily meteorological data, including precipitation, temperature, relative humidity, wind speed and sunshine hours were collected at 743 national meteorological stations during 1961–2010 from the China Meteorological Administration. In addition, daily solar radiation was collected from 118 stations during the period 1961–2010. Meanwhile, monthly runoff data of 282 catchments across China were collected. These catchments were selected based on the length of records exceeding 25 years and all observed points being within the supply and demand limits of the framework. Furthermore, there is relatively low direct influence of human activities such as, irrigation, damming, and water diversion on the catchments. The areas of these catchments vary from 372 to 142,963 km\(^2\) and these catchments cover a sizable portion of land area within China as shown in Fig. 1. The catchment average slope was calculated from the HYDRO1k data sets, developed by the US Geological Survey’s (USGS) Earth Resources Observation and Science (EROS) Data Cen-
ter, at a resolution of 1 km. (available at http://eros.usgs.gov/
elevation-products).

Because the precipitation type has not been available at
any of the meteorological stations since 1980, the empirical
relationship evaluated for the Chinese territory to discrimi-
nate precipitation types is called for. The empirical discrimi-
nation scheme (Ding et al., 2014) derived from more than
400 000 samples collected from different climate regimes
and elevations across China from 1951 to 1979 was adopted.
The precipitation is categorized according to

\[
\text{type} = \begin{cases} 
\text{snow}, & T_w \leq T_1 \\
\text{sleet}, & T_1 \leq T_w \leq T_2 \\
\text{rain}, & T_w \geq T_2 
\end{cases}
\]

where \(T_w\) is daily mean wet-bulb temperature, a function of
air temperature, relative humidity and air pressure. \(T_1\) and
\(T_2\) are two threshold temperatures which can be empirically
parameterized by relative humidity and elevation based on
the observations. According to this discrimination scheme, if
a precipitation event was judged as snow or sleet, the cor-
responding precipitation quantity was counted in the annual
snowfall amount.

To obtain the average daily climate forcing in each catch-
ment, a 10 km grid data across the China was interpolated
from the observations of all meteorological stations by angu-
lar distance-weighted interpolation, and then catchment val-
ues were calculated by averaging values of grids covering
the analyzed catchments. The interpolated grid temperature
was modified by its elevation. Daily \(E_p\) was calculated based
on the Penman–FAO equation (Allen et al., 1998) using grid
data with consideration of the corresponding land use type.
And the \(E_p\) of grids which are water and non-water were cal-
culated using Eqs. (2) and (3), respectively.

\[
E_p = \frac{\Delta}{\Delta + \gamma} \left( \frac{R_a - G}{\lambda} \right) + \frac{\Delta}{\Delta + \gamma} \left( \frac{6.43(1 + 0.536U_2)(e_s - e_a)}{\lambda} \right),
\]

(2)

\[
E_p = 0.408 \frac{\Delta}{\Delta + \gamma^*} \left( R_a - G \right) + \frac{\gamma}{\Delta + \gamma^*} \left( \frac{900}{T + 273} U_2 \right) (e_s - e_a),
\]

(3)

where \(T\) is daily average air temperature [°C] and \(\Delta\) is the
slope of the saturated vapor pressure versus \(T\) curve
[kPa °C⁻¹]; \(U_2\) is the wind speed at 2 m above ground
[m s⁻¹]; \(e_s\) is the saturated vapor pressure [kPa]; \(e_a\) is the
actual vapor pressure [kPa]; \(R_a\) and \(G\) are the net radia-
tion and ground heat flux, respectively [MJ m⁻² d⁻¹]; \(\lambda\) is the latent
heat of vaporization of water [J g⁻¹] and \(\gamma\) is the psychome-
tric constant [kPa °C⁻¹]. \(\gamma^* = \gamma (1 + 0.34 U_2)\).

The daily climate variables were aggregated to annual val-
ues for all catchments. The snow ratio (\(r_s\)) was calculated as
the ratio of mean annual snowfall amount to mean annual
precipitation, which can eliminate the influence of phase dif-
fERENCE originating from the snow accumulation and melting
in different years.

The monthly Global Inventory Modeling and Mapping
Studies (GIMMS) normalized difference vegetation index
(NDVI) from 1982 to 2006 with 8 km resolution was col-
lected from the Advanced Very High Resolution Radiometer
(AVHRR) sensor (Buermann et al., 2002). Likewise, long-
term average annual NDVI value for each catchment was
calculated from the data set and the corresponding vegeta-
tion coverage (\(M\)) was estimated following Gutman and Ig-
natov (1998):

\[
M = \frac{\text{NDVI} - \text{NDVI}_{\text{min}}}{\text{NDVI}_{\text{max}} - \text{NDVI}_{\text{min}}},
\]

(4)

where \(\text{NDVI}_{\text{max}}\) and \(\text{NDVI}_{\text{min}}\) are the NDVI signals from
dense green vegetation and bare soil, which were chosen to
be 0.80 and 0.05, respectively (Yang et al., 2009).

The future climate forcing, monthly precipitation, tem-
perature and snowfall outputs of all the available ex-
periments from two representative concentration pathways
(RCPs) archived in the Coupled Model Intercomparison
Project Phase 5 (CMIP5) (Taylor et al., 2012) were extracted
(38 GCMs for RCP4.5; 40 GCMs for RCP8.5, as shown in
Table 1). For each GCM and each RCP, the precipitation,
temperature and snowfall outputs at the archived spatial res-
olution were regirded to 0.5° × 0.5° grid cells. For each
catchment, the monthly areal average precipitation, tem-
perature and snowfall from 2050 to 2099 were calculated from
above model outputs. Monthly \(E_p\) was computed using the
Hamon’s equation (Hamon, 1961) as

\[
E_p = \alpha \cdot d \cdot D^2 \cdot \rho_w,
\]

(5)

where \(d\) is the number of days in a month, \(D\) is the
mean monthly hours of daylight in units of 12 h,
\(\rho_w = 0.0495 e^{0.006T}\) is a saturated water vapor density
and \(T\) is the monthly mean temperature [°C]. \(\alpha\), the adjust-
ment factor, was calibrated via minimizing the difference be-
tween the two mean annual \(E_p\) values (2000–2010) obtained by
the Penman–FAO and Hamon’s equation for each catchment.
The projected monthly precipitation, snowfall and poten-
tial evapotranspiration were aggregated to annual values for
2050–2099.

3 Methodology

3.1 Inclusion of snow ratio in the Budyko framework

At multi-decade timescales, neglecting the catchment
groundwater or glacial storage change, mean annual actual
\(E\) is estimated as the residual of annual precipitation minus
runoff (\(Q\)). On the other hand, \(E\) can be given by a function
of available energy (\(E_p\)) and available water (\(P\)) for evapo-
transpiration, proposed by Budyko (1974):

\[
1 - \frac{Q}{P} = \sqrt{\frac{E_p}{P} \left[ 1 - \exp \left( -\frac{E_p}{P} \right) \right] \tanh \left( \frac{1}{E_p/P} \right)}.
\]

(6)

Other Budyko-type curves were developed for describing
catchment long-term water balance, by introducing a unique
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Table 1. Overview of selected GCMs used in climate impact assessment. More details of the models, modeling centers and meaning of the ensemble codes can be found at http://cmip-pcmdi.llnl.gov/cmip5/availability.html.

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1 - \frac{Q}{P} = \left[ 1 + \left( \frac{E_p}{P} \right)^{-n} \right]^{-1/n}, \quad (7)

where n is a synthesis parameter which represents the effects of catchment factors (i.e., vegetation type and coverage, soil type and topography) on the precipitation partitioning, referred to as the specific catchment parameter herein. As shown in Fig. 2, the relationship between mean annual runoff index (Q/P) and dryness index (E_p/P) is depicted.
A larger value of \( n \) is associated with a lower runoff index given the same dryness index.

When snowfall is considered, there are some differences in energy and water terms involved in Eq. (7). For evapotranspiration capacity, it should be noted that part of the available energy which needs to be taken away to melt the snowfall compared with “paired catchment” where other conditions are the same but all precipitation falls as rainfall. Meanwhile, little sublimation and runoff are observed during snow accumulation season (Anderson, 1968; Dewalle and Meiman, 1971; Weller and Holmgren, 1974). The snowfall needs to be transferred into liquid phase before it can participate in the hydrological cycle. The melting energy \( R_m \) required to convert snowfall to the reference state (0°C liquid phase) reads

\[
R_m = \rho_w W (h_f + C_i \Delta T),
\]  

where \( \rho_w \) is the density of water [1000 kg m\(^{-3}\)]; \( W \) is snow water equivalence [m], i.e., snowfall amount \((r_s \cdot P)\); \( h_f \) is the latent heat of fusion [335 kJ kg\(^{-1}\)]. \( C_i \Delta T \) represents the energy needed in snow warming phase during which the average accumulated snow temperature increases until the snowpack is isothermal at 0°C where \( C_i \) is the specific heat of ice [2.1 kJ kg\(^{-1}\) °C\(^{-1}\)] and \( \Delta T \) average negative snow surface temperature, order of 10°C.

Thus, the effective energy available for evapotranspiration \( E^e_p \) is the difference between \( E_p \) and melting heat equivalence \( R_m / L \), where \( L \) is latent heat of evaporation [2500 kJ kg\(^{-1}\)]. After a rough algebraic computation, \( E^e_p \) reads

\[
E^e_p = E_p - \frac{R_m}{L} = E_p - 0.14r_s \cdot P.
\]  

In melting season, the magnitude of sensible heat is several times larger than latent heat (Dingman, 2002), implying that only a small part of snow is evaporated or sublimated. For example, according to the energy budget during the accumulation and melt periods for six seasons (1968–1973) at the Danville site, VT, USA (Anderson, 1976), the average turbulent exchange of latent heat in each season are 1160 cal cm\(^{-2}\), equivalent to 1.7 cm vaporized water. Compared with the maximum snow depth of 72 cm in that location, the evaporation of snowfall is very small.

Furthermore, the concrete frozen ground is most commonly found in open land and sometimes in forested land (Pierce et al., 1958; Fahey and Lang, 1975), which makes the melting water infiltration difficultly. Given that the frozen ground has extremely low permeability, the surface flow is preferred during the snow melting period (Dunne and Black, 1971); moreover, the melting snowfall accumulates to form a basal saturated zone through which water drains to the stream (Anderson, 1976). Therefore, it is acceptable to assume that melting snow water flows away through channels without evaporation loss. As a consequence, the effective available water for evapotranspiration is annual rainfall \((1 - r_s) \cdot P\), rather than total precipitation \( P\).

The water–energy balance in form of Eq. (7) with consideration of snow can be rewritten as follows:
the revised dryness index is about an order of 0.01, and can be neglected compared with pre- and post-period due to variations of precipitation, potential evapotranspiration, snow ratio and catchment parameter, respectively. Specifically, relative contribution of snow ratio variation to annual runoff change, \( \eta_{rs} \), is defined as

\[
\eta_{rs} = \frac{\Delta Q_{rs}}{\Delta Q} \cdot \left| \frac{\Delta Q}{Q_1} \right| = \text{sgn}(\Delta Q) \cdot \frac{\Delta Q}{Q_1},
\]

where \( \Delta Q_{rs} = \frac{\Delta E_p}{\Delta r_s} \Delta r_s \); \( \Delta Q = Q_2 - Q_1 \) and \( \Delta r_s = r_{s2} - r_{s1} \) represent difference between post- and pre-period recorded mean annual runoff and snow ratio, respectively; \( \Delta n' \) represents change in land cover and can be calculated using the mean annual \( P \) and \( E_p \), as well as \( r_s \) for each sub-period by Eq. (11).

### 4 Results and discussion

#### 4.1 Effect of snow ratio on runoff

\( Q/P \) of the 282 catchments is plotted in Fig. 2 as a function of \( E_p/P \). Each point represents a mean annual record for one basin with different colors indicating the various snow ratios. The dashed lines are derived from Eq. (7) with different specific catchment parameter, by neglecting changes in catchment storage at the mean annual scale. There is a general pattern that the catchments with a larger snow ratio have higher runoff index for a given dryness index, which is consistent with the finding from data set in the USA (Berghuijs et al., 2014). However, it is still not clear that the different snow ratios of each catchment result in this kind of variance in runoff index. Before we can make this conclusion, effects of other factors on runoff index need to be excluded.

Due to limitation of available catchment data, as well as recent studies implying that the vegetation coverage (Donohue et al., 2007; Voepel et al., 2011; Xu et al., 2013) and average slope (Yang et al., 2009, 2014a) of catchment may be the key control on long-term hydrologic partitioning of precipitation, we assume that vegetation coverage and average slope can be thought of as two integrators of catchment properties. We estimated the specific catchment parameter \( n \) in Eq. (7) from historical observations for each catchment. In order to clear away the impacts that catchment local characteristics (herein the vegetation cover and slope are thought as the proxy of integral characteristics) have on runoff, all catchments are divided into four groups, and catchments in the same group share the similar vegetation coverage or slope. Pearson’s linear correlation between the specific catchment parameter \( n \) and the snow ratio in the same group is calculated, by which we can tell whether the snow ratio still has a significant impact on catchment water-energy balance after getting rid of the influence of local catchment properties. Figures 3 and 4 show how specific catchment parameters vary with different snow ratios in each group with similar catchment vegetation cover and average slope, respectively. The results suggest that for those catchments with similar local catchment properties, catchments with a higher snow ratio tend to have a
Figure 3. In the context of the Budyko–Choudhury framework, statistical relationships between the specific catchment parameter $n$ and the snow ratio, under similar vegetation coverage. Least squares regression lines are shown on each of the plots. The Pearson’s linear correlation coefficient clarifies the significant negative correlation between snow ratio and catchment parameter. (a–d) indicate the vegetation coverage of <0.3, (0.3, 0.4), (0.4, 0.5), and >0.5, respectively.

Figure 4. Similar with Fig. 3 for catchment average slope. (a–d) indicate the average slope (%) of (0.2, 3.8), (3.8, 5.5), (5.5, 8.0), and >8.0, respectively.
smaller specific catchment parameter \( n \). Moreover, the notable negative correlation between catchment parameter \( n \) and the snow ratio can be seen in the catchments under small and medium vegetation cover (Fig. 3a–c), or large average slope (Fig. 4d).

In other words, when excluding the effects of local catchment characteristics, catchments with a larger snow ratio are believed to yield more runoff under the same climatological condition. With the above analysis, we can make a more solid conclusion that the snow ratio itself indeed has impact on mean annual runoff in the context of the Budyko hypothesis. Changes in the state of precipitation from snow to rainfall not only affect the seasonal runoff dynamics but also alter the mean annual runoff amount. Accordingly, how to evaluate the effects of snow ratio on annual runoff variance is meaningful. Furthermore, quantifying the sensitivity of annual runoff to snow ratio using a new approach based on the Budyko hypothesis, instead of employing least squares estimators of historical records (Berghuijs et al., 2014), may provide more insight into this phenomenon. Therefore, much more elaboration with physic mechanism, like proposed in Sect. 3.1, is needed to build.

4.2 Validity of the Budyko framework considering snow effects

We estimated the catchment parameter \( n' \) in Eq. (11), and then evaluated the method’s validity by investigating the relationship between \( n' \) and snow ratio. As shown in Table 2, the correlation between \( n' \) value and snow ratio for each catchment was calculated. The correlation approximates to zero and is insignificant, when taking all 282 catchments as a whole. Furthermore, when catchments are grouped by vegetation coverage as in Sect. 4.1, no significant negative correlation is detected, except for group with vegetation coverage of 0.4–0.5, and the findings are similar for catchment groups classified by slope.

4.3 Contribution of climate and land use change to runoff

The annual runoff experiences a downward (decreasing) step change across China around 1980 (Zhang et al., 2008). The change in mean annual runoff is calculated as the difference between the period of 1980–2005 and the period of 1956–1979. As shown in Fig. 5, most of the study catchments show a decreasing runoff change rate, defined as the ratio of runoff change between two periods to mean annual runoff.

Table 2. Summary of correlation between specific catchment parameter and snow ratio for different catchment groups – \( n \) is estimated by Eq. (7); \( n' \) is estimated by Eq. (11).

<table>
<thead>
<tr>
<th></th>
<th>All 282 catchments</th>
<th>Catchments with ( r_s &gt; 0.01 )</th>
<th>Catchments with ( r_s &gt; 0.02 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( n )</td>
<td>( -0.21^{***} )</td>
<td>( -0.27^{***} )</td>
<td>( -0.38^{***} )</td>
</tr>
<tr>
<td>( n' )</td>
<td>0.05</td>
<td>0.04</td>
<td>0.03</td>
</tr>
<tr>
<td>Vegetation coverage</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.1–0.3</td>
<td>( -0.50^{***} )</td>
<td>( -0.50^{***} )</td>
<td>( -0.50^{***} )</td>
</tr>
<tr>
<td>0.3–0.4</td>
<td>( -0.49^{***} )</td>
<td>( -0.44^{***} )</td>
<td>( -0.48^{***} )</td>
</tr>
<tr>
<td>0.4–0.5</td>
<td>( -0.44^{***} )</td>
<td>( -0.47^{***} )</td>
<td>( -0.59^{***} )</td>
</tr>
<tr>
<td>0.5–0.7</td>
<td>( -0.09 )</td>
<td>0.03</td>
<td>0.04</td>
</tr>
<tr>
<td>Slope (%)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.2–3.8</td>
<td>( -0.24^{*} )</td>
<td>( -0.25^{*} )</td>
<td>( -0.30^{**} )</td>
</tr>
<tr>
<td>3.8–5.5</td>
<td>( -0.14 )</td>
<td>( -0.06 )</td>
<td>( -0.16 )</td>
</tr>
<tr>
<td>5.5–8.0</td>
<td>( -0.20 )</td>
<td>( -0.35^{***} )</td>
<td>( -0.41^{***} )</td>
</tr>
<tr>
<td>8.0–18.7</td>
<td>( -0.40^{***} )</td>
<td>( -0.47^{***} )</td>
<td>( -0.45^{***} )</td>
</tr>
</tbody>
</table>

Note: *, ** and *** indicate the significant level at 0.05, 0.01 and 0.001, respectively.
The modeled runoff change is calculated by Eq (13). Figure 6 shows the comparison between modeled runoff changes and that observed for all 282 catchments. The points scatter overall along with the 1 : 1 line, indicating the proposed attribution method has a good performance for most catchments and it is convincing to analyze the relative contribution of each variable to mean annual runoff variation using this method.

The relative contributions of four factor variations to the annual runoff change are depicted in Fig. 7. During the past 50 years, total precipitation amount across China has no obvious trend, while increasing winter precipitation is seen in parts of the northern high latitude and mountains (Sun et al., 2010; Zhang and Cong, 2014). As a result, it is obvious that a significant effect of change in the snow ratio on annual runoff alteration is found in northwestern mountainous and high-latitude catchments (Fig. 7a) where a larger portion of winter precipitation falls in a solid state. Generally, the increasing snow ratio makes a negative contribution to the observed decreasing mean annual runoff; there is no general spatial pattern where change in total precipitation has a remarkable contribution to annual runoff alteration (Fig. 7b). During the past 3 decades, northern China, especially the North China
Figure 7. Relative contributions of (a) snow ratio, (b) precipitation, (c) specific catchment parameter, and (d) potential evapotranspiration variance to change in mean annual runoff. Upward triangle represents the positive relative contribution of the variable to change in runoff, while downward triangle represents the negative.

Plain (Liu et al., 2003), has been seeing significant land use and land cover change, including urbanization and afforestation. Therefore, a large difference of catchment property $n$ between two studied periods is expected. Among the four variables, the catchment parameter (Fig. 7c) has most significant effects on mean annual runoff change. In most parts of China, the annual $E_p$ shows a decreasing trend, but the decreasing magnitude between post- and pre-period is negligible (Gao et al., 2006). As expected, the overall small negative ($<15\%$) or tiny relative contribution of decreasing $E_p$ to decreasing mean annual runoff is shown in Fig. 7d.

### 4.4 Plausible future runoff changes

As far as we are concerned, in a plausible future warming climate, quantifying the change in annual runoff resulting from per unit variation in the fraction of precipitation falling as snow is particularly vital for water resources planning. An insight into possible influence of future changing climate, especially snow ratio on annual runoff, is provided here. The 2050–2099 average annual precipitation, snow ratio and $E_p$ of each catchment estimated from the multi-model ensemble average values are used as climate forcing to calculate corresponding catchment’s future mean annual runoff by Eq. (11), assuming unchanged catchment parameter $n'$ estimated from the past-decade observed data.

The projected mean annual runoff increase for 2050–2099 relative to 1956–2005 is widespread in northern China (Fig. 8). On the other hand, a slight decrease is projected in most regions of southern China. The spatial pattern of the projected runoff change is consistent with runoff outputs from atmosphere–ocean general circulation models participating in the CMIP5 (Koirala et al., 2014). The runoff increase projection in parts of northern China mainly results...
from future increasing precipitation amount, as well as the increasing snowfall, which is also reported by other climate change impact assessments in East Asia (Immerzeel et al., 2013). As shown in Fig. 9, the contribution of snow ratio to runoff change, defined as the ratio of runoff change due to snow ratio change to the total runoff change, is overall positive and pronounced over the catchments located in northern high-latitude and northwestern mountainous regions. The regions are consistent with areas where catchment runoff is sensitive to snow ratio variation over the past several decades as shown in Fig. 7a. Moreover, the patterns of snow ratio’s contribution to runoff for RCP4.5 and RCP8.5 scenarios bear some overall resemblance, including the sensitive areas and magnitudes. Also, some differences exist where snow ratio change contributes more to runoff increasing for RCP4.5 than RCP8.5, mainly in central China. Specifically, the snow ratio’s contribution to runoff change for RCP4.5 is overall larger than that for RCP8.5, although the differences are insignificant (Fig. 10). It indicates that simulated climate outputs forced with a mid-range mitigation emissions scenario (RCP4.5) tend to more runoff and larger snow ratio’s contribution to runoff change in China, compared with that under a high-emissions scenario.

4.5 Error analysis of attribution method

Since only the first-order approximation of runoff change is used to calculate the contribution of each variable in the attribution method Eq. (13), we conduct the error analysis to access its performance in the following. Similar with Yang et al. (2014a), the Taylor series of Eq. (12) is employed to show the complete expression of runoff change as

Figure 8. Change rate of mean annual runoff under projected future climate. (a) RCP4.5 and (b) RCP8.5.
The runoff change induced by the snow ratio change can be expressed as

\[
Q (P_1 + \Delta P_1, E_{p1}, r_{s1}, n_1) = Q (P_1, E_{p1}, r_{s1}, n_1) + \left( \Delta P_1 \frac{\partial}{\partial P_1} + \Delta E_{p1} \frac{\partial}{\partial E_{p1}} + \Delta r_{s1} \frac{\partial}{\partial r_{s1}} + \Delta n_1 \frac{\partial}{\partial n_1} \right) \cdot Q (P_1, E_{p1}, r_{s1}, n_1) + \cdots 
\]

(16)

The runoff change induced by the snow ratio change can be expressed as

\[
Q (P_1 + \Delta P_1, E_{p1}, r_{s1}, n_1) = Q (P_1, E_{p1}, r_{s1}, n_1) + \left( \Delta P_1 \frac{\partial}{\partial P_1} + \Delta E_{p1} \frac{\partial}{\partial E_{p1}} + \Delta r_{s1} \frac{\partial}{\partial r_{s1}} + \Delta n_1 \frac{\partial}{\partial n_1} \right) \cdot \frac{\partial Q}{\partial r_{s1}} (P_1, E_{p1}, r_{s1}, n_1) + \cdots 
\]

(17)

where we neglect the third- and higher-order terms of Eq. (16) for the third order is equal to 3% of the second order according to Yang et al. (2014b). The relative error (RE) of attribution method to investigate the contribution of snow ratio change is estimated as

\[
\text{RE}_{\Delta r_{s1}} = \left| \frac{\Delta Q_{\Delta r_{s1}} - \Delta Q_{r_{s1}}}{\Delta Q_{\Delta r_{s1}}} \right| \cdot \left| \frac{\Delta Q_{r_{s1}}}{\Delta Q_{\Delta r_{s1}}} \right|. 
\]

(18)

As shown in Fig. 11, the relative errors of attribution method with respect to snow ratio change are small for all 282 catchments. Specifically, as for the contribution of snow ratio...
change to the historical runoff, the RE of more than 90% of catchments is no more than 11%. As to the two projected future climate change scenarios, the REs of more than 90% of catchments are less than 8 and 12% for RCP4.5 and RCP8.5, respectively. Therefore, the proposed first-order approximation attribution method is reliable.

4.6 Limitation of revised Budyko framework

It should be noted that the assumption of no evapotranspiration loss in snowmelt adopted in Sect. 3.1 is not universally applicable. In small catchments, after snowfall is melt and the concrete frozen ground inhibits snowmelt infiltration, the snow water can flow away quickly through channels without evaporation loss. However, if the location of
accumulated snow is far away from channels, or the snowfall amount is large, it will take longer for meltwater to run off than the frozen soil thaws. In these cases, a part of snow infiltrates into the ground and later is available for evaporation (Dripps, 2012; Jasechko et al., 2014). In fact, it may be more suitable to introduce as effective available water for evapotranspiration, where k is a loss parameter requiring further investigation. To better understand and parameterize the snowmelt loss by evapotranspiration, the site-specific modeling and isotope-based field observations may provide tools for more detailed modeling in the future.

Apart from limitation of the assumption, the accurate estimation of snow ratio is also important for this framework. However, direct snow observation records are not available for the case study watersheds in this manuscript and the MOPEX watersheds used by Berguijs et al. (2014). Mean annual snowfall is estimated by the air temperature-based empirical method. The threshold temperature is critical for calculating the snowfall amount. A higher threshold temperature will overestimate the snow ratio that may lead to an unreasonable conclusion under the framework in our study. According to the sensitivity analysis of catchment parameter estimation, it shows that a small variation in snow ratio can lead to a significant change in catchment parameter when snow ratio is large enough to be comparable to runoff index. Thus, the accuracy of snow ratio is important to this framework especially when the snow ratio is large, which limits the applicability of this framework in those catchments.

5 Conclusions

In this study, we showed that the snow ratio could have a pronounced effect on mean annual runoff based on both historical records and theoretical analysis. In the context of the Budyko hypothesis, catchments with a larger snow ratio tend to yield more long-term mean annual runoff given the same other climatological and landscape properties. Moreover, a Budyko-type equation considering the water–energy balance is derived to quantify the effects of snow ratio on runoff. With the assistance of the proposed relationship, the contribution of snow ratio to change in annual runoff during the past 5 decades and potential annual runoff variation due to changing fraction of precipitation falling as snow under a projected future global warming scenario in China are investigated. The results indicate that those sensitive catchments in northwestern mountainous and north-central high-latitude areas are undergoing remarkable runoff change resulting from snow ratio variance. In addition, the error analysis of attribution method is conducted, implying that the first-order approximation is suitable to assess the contribution of snow ratio change to runoff in this study.

This paper extends the previous work that suggested that precipitation shift from snow towards rain leads to a decrease in runoff based on a data set in USA (Berghuijs et al., 2014). We confirm here that the observations in China give a similar conclusion. Furthermore, we quantify this effect and assess the impact of climate change, especially snow ratio change, on mean annual runoff across China. As major rivers originating from mountainous regions where temperature determines the state of precipitation (Allamano et al., 2009) and afterwards affects annual runoff amount as discussed above, the findings here have valuable implications for future water management policy. The proposed model can be made applicable to other mountainous catchments of the world easily and quantify the effects of possible change in the snow ratio on available water resources and analyze the vulnerability of catchments to climate change.

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D. Zhang et al.: Effects of snow ratio on annual runoff within the Budyko framework


